

Chapter 2

Chemical Formulas, Chemical Equations, and Reaction Yields

- 2.2 Find the mass fractions by dividing the mass of each element present in a mole of acetaminophen (N-acetyl-*p*-aminophenol, $C_8H_9NO_2$) by the molar mass

$$f_C = \frac{8 \times 12.011 \text{ g mol}^{-1}}{151.165 \text{ g mol}^{-1}} = 0.6356 \quad f_H = \frac{9 \times 1.00794 \text{ g mol}^{-1}}{151.165 \text{ g mol}^{-1}} = 0.06001$$

$$f_N = \frac{1 \times 14.0067 \text{ g mol}^{-1}}{151.165 \text{ g mol}^{-1}} = 0.09266 \quad f_O = \frac{2 \times 15.9994 \text{ g mol}^{-1}}{151.165 \text{ g mol}^{-1}} = 0.2117$$

The mass percentages equal the mass fractions multiplied by 100%.

- 2.4 Save work by *estimating* the fluorine content of each compound. Thus, HF is certainly the compound richest in fluorine by mass because the only other atom in its formula is the very light hydrogen atom—there is only 1 unit of non-fluorine mass per fluorine atom. The non-fluorine mass per fluorine atom in C_6HF_5 is about $(6 \times 12)/5 \approx 14$; in BrF it is 79.9; in UF_6 it is $238/6 \approx 40$. The desired order is therefore $BrF < UF_6 < C_6HF_5 < HF$.
- 2.6 The pharmacist mixes 286 g of Na_2CO_3 with 150 g of $C_2H_5NO_2$, using water as a mixing agent. After all the water is driven away, the mixture weighs 436 g. The mass of carbon from the Na_2CO_3 is $(12.011/105.988) \times 286$ g; the mass of carbon from the $C_2H_5NO_2$ is $(2 \times 12.011/75.067) \times 150$ g where the 105.988 and 75.067 are the respective molecular masses of the compounds. The mass of carbon in the mixture is the sum of these two masses. It equals 80.412 g. The mass percentage of carbon is this mass divided by 436 g and multiplied by 100%. It is 18.4%.
- 2.8 Imagine 100.0 g of bromoform. The mass of bromine is 94.85 g, the mass of hydrogen is 0.40 g, and the mass of carbon is 4.75 g. Convert each of these masses to chemical amount by dividing by the molar mass of the element: there are 1.18705 mol of Br, 0.39685 mol of H, and 0.39547 mol of C. (Nonsignificant figures appear in these intermediate values for the sake of greater precision in the final result.) The three chemical amounts stand in the ratio of 2.99 to 1.003 to 1. Within the precision of the data this ratio is 3 to 1 to 1. The empirical formula is Br_3HC .
- 2.10 Imagine 100.0000 g of the compound. This sample contains 1.6907 g of O and 98.3093 g of Cs. The chemical amount of oxygen is its mass divided by its molar mass; it equals 0.10567 mol. The chemical amount of cesium is 0.73969 mol. The ratio of the chemical amounts is 7.000 to 1, making the empirical formula Cs_7O .

2.12 The empirical formulas of the five compounds are

A. CO₂, B. CO₁, C. C₄O₃, D. C₃O₂, E. C₅O₂

All five of these compositions exist. The first two are well-known. The third is mellitic anhydride (molecular formula C₁₂O₉). The last two are carbon suboxides having molecular formulas identical to their empirical formulas.

2.14 Compare the chemical amounts of the three elements in the compounds

$$\begin{aligned}n_{\text{Ca}} &= n_{\text{CaO}} = \frac{2.389 \text{ g}}{56.0774 \text{ g mol}^{-1}} = 0.04260 \text{ mol} \\n_{\text{C}} &= n_{\text{CO}_2} = \frac{1.876 \text{ g}}{44.010 \text{ g mol}^{-1}} = 0.04263 \text{ mol} \\n_{\text{N}} &= n_{\text{NO}_2} = \frac{3.921 \text{ g}}{46.0055 \text{ g mol}^{-1}} = 0.08523 \text{ mol}\end{aligned}$$

Divide each of these amounts by the smallest. The resulting ratios are 1 : 1.001 : 2.001. This means that the empirical formula is CaCN₂

2.16 Two gases held at the same conditions contain the same number of molecules per unit volume. This means that the ratio of molar masses of these two gases equals the ratio of their densities:

$$\frac{M_{\text{P}_n}}{M_{\text{N}_2}} = \frac{2.7 \text{ g L}^{-1}}{0.62 \text{ g L}^{-1}} \text{ hence } M_{\text{P}_n} = \left(\frac{2.7}{0.62}\right)(28.014 \text{ g mol}^{-1}) = 1.2 \times 10^2 \text{ g mol}^{-1}$$

The molar mass of atomic P is only 30.97 g mol⁻¹. The P₄ molecule however has a molar mass of 124 g mol⁻¹, which equals 1.2 × 10² g mol⁻¹ within the precision of the data (two significant digits). Conclude that there are four P atoms per molecule under these conditions.

2.18 a) The relative molecular mass of the binary compound is (2.53) (28.013) = 70.9.

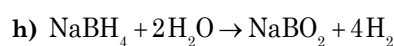
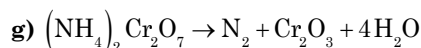
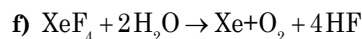
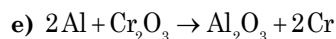
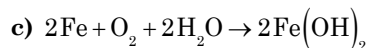
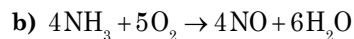
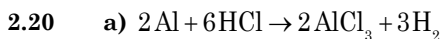
b) Each molecule of the compound has one N atom because

$$\frac{8.21 \text{ g}}{70.9 \text{ g mol}^{-1}} = 0.116 \text{ mol compound contains } \frac{1.62 \text{ g}}{14.007 \text{ g mol}^{-1}} = 0.116 \text{ mol N}$$

c) The maximum possible value of the relative atomic mass of the other element is 70.9 – 14.0 = 56.9.

d) Divide 56.9 by the positive integers: 56.9/2 = 28.5; 56.9/3 = 19.0; 56.9/4 = 24.2, and so forth. Compare the results to the known relative atomic masses. The closest fit is F (relative atomic mass 19.0).

e) NF₃



2.22 a)

$$m_{\text{Ca}(\text{OH})_2} = \left(\frac{1.000 \text{ g CaCO}_3}{100.09 \text{ g mol}^{-1}}\right) \left(\frac{1 \text{ mol Ca}(\text{OH})_2}{1 \text{ mol CaCO}_3}\right) \times 74.094 \text{ g mol}^{-1} = 0.7403 \text{ g}$$

b)

$$m_{\text{CO}_2} = \left(\frac{1.000 \text{ g C}_3\text{H}_8}{44.096 \text{ g mol}^{-1}} \right) \left(\frac{3 \text{ mol CO}_2}{1 \text{ mol C}_3\text{H}_8} \right) \times 44.010 \text{ g mol}^{-1} = 2.994 \text{ g}$$

c)

$$m_{\text{Mg}_2\text{P}_2\text{O}_7} = \left(\frac{1.000 \text{ g MgNH}_4\text{PO}_4}{137.315 \text{ g mol}^{-1}} \right) \left(\frac{1 \text{ mol Mg}_2\text{P}_2\text{O}_7}{2 \text{ mol MgNH}_4\text{PO}_4} \right) \times 222.55 \text{ g mol}^{-1} = 0.8104 \text{ g}$$

2.24 Whatever the reaction or series of reactions that gives $\text{Pt}_2\text{C}_{10}\text{H}_{18}\text{N}_2\text{S}_2\text{O}_6$, the chemical amount that forms cannot exceed half the chemical amount of platinum because the compound contains two Pt per molecule. Thus

$$m_{\text{cmpd}(\text{max.})} = 1.406 \text{ g Pt} \times \frac{1 \text{ mol Pt}}{195.08 \text{ g Pt}} \times \frac{1 \text{ mol Pt}_2\text{C}_{10}\text{H}_{18}\text{N}_2\text{S}_2\text{O}_6}{2 \text{ mol Pt}} \\ \times \frac{716.55 \text{ g Pt}_2\text{C}_{10}\text{H}_{18}\text{N}_2\text{S}_2\text{O}_6}{1 \text{ mol Pt}_2\text{C}_{10}\text{H}_{18}\text{N}_2\text{S}_2\text{O}_6} = 2.582 \text{ g Pt}_2\text{C}_{10}\text{H}_{18}\text{N}_2\text{S}_2\text{O}_6$$

2.26 Use the balanced equation $\text{Si}_4\text{H}_{10} + \frac{13}{2}\text{O}_2 \rightarrow 4\text{SiO}_2 + 5\text{H}_2\text{O}$

$$m_{\text{SiO}_2} = 25.0 \text{ cm}^3 \text{ Si}_4\text{H}_{10} \times \frac{0.825 \text{ g}}{1 \text{ cm}^3} \times \frac{1 \text{ mol}}{122.42 \text{ g}} \times \frac{4 \text{ mol SiO}_2}{1 \text{ mol Si}_4\text{H}_{10}} \times \frac{60.0843 \text{ g SiO}_2}{1 \text{ mol SiO}_2} \\ = 40.5 \text{ g SiO}_2$$

2.28

$$m_{\text{CS}_2} = 67.2 \text{ g S} \times \frac{1 \text{ mol S}}{32.066 \text{ g S}} \times \frac{1 \text{ mol CS}_2}{4 \text{ mol S}} \times \frac{76.143 \text{ g CS}_2}{1 \text{ mol CS}_2} = 39.9 \text{ g CS}_2$$

2.30

$$m_{\text{Ca}_3(\text{PO}_4)_2} = 69.8 \text{ g P}_4 \times \frac{1 \text{ mol}}{123.895 \text{ g}} \times \frac{2 \text{ mol Ca}_3(\text{PO}_4)_2}{1 \text{ mol P}_4} \times \frac{310.18 \text{ g}}{1 \text{ mol}} = 349 \text{ g Ca}_3(\text{PO}_4)_2 \\ m_{\text{CaSiO}_3} = 69.8 \text{ g P}_4 \times \frac{1 \text{ mol}}{123.895 \text{ g}} \times \frac{6 \text{ mol CaSiO}_3}{1 \text{ mol P}_4} \times \frac{116.16 \text{ g}}{1 \text{ mol}} = 393 \text{ g CaSiO}_3$$

2.32 a) Let M_A represent the molar mass of element A. Then $M_A + 3(126.90) \text{ g mol}^{-1}$ is the molar mass of Al_3 and $M_A + 3(35.453) \text{ g mol}^{-1}$ is the molar mass of AlCl_3 . Use the stoichiometry of the equation

to express the mass of AlCl_3 obtained in terms of the mass of Al_3 treated

$$0.3776 \text{ g} = 0.8000 \text{ g Al}_3 \times \frac{1 \text{ mol Al}_3}{(M_A + 380.7) \text{ g Al}_3} \times \frac{1 \text{ mol AlCl}_3}{1 \text{ mol Al}_3} \times \frac{(M_A + 106.36) \text{ g AlCl}_3}{1 \text{ mol AlCl}_3}$$

Which becomes

$$0.8000(M_A + 106.36) = 0.3776(M_A + 380.7) \quad \text{from which} \quad M_A = 138.9 \text{ g mol}^{-1}$$

b) The element is lanthanum, La.

2.34 Express the amount of hydrogen that is evolved as a chemical amount

$$n_{\text{H}_2} = \frac{0.738 \text{ g}}{2.016 \text{ g mol}^{-1}} = 0.366 \text{ mol H}_2$$

Let the mass of iron in the original mixture be represented by x . Then

$$n_{\text{Fe}} = \frac{x \text{ g Fe}}{55.845 \text{ g mol}^{-1}} \quad \text{and} \quad n_{\text{Al}} = \frac{(9.62 - x) \text{ g Al}}{26.982 \text{ g mol}^{-1}}$$

The 0.366 mol of H_2 is evolved by these molar amounts of Fe and Al in reaction with excess HCl according to the equations given in the problem. Determine the molar amount of H_2 that each metal produces and add them

$$\frac{x \text{ g Fe}}{55.845 \text{ g mol}^{-1}} \left(\frac{1 \text{ mol H}_2}{1 \text{ mol Fe}} \right) + \frac{(9.62 - x) \text{ g Al}}{26.982 \text{ g mol}^{-1}} \left(\frac{3 \text{ mol H}_2}{2 \text{ mol Al}} \right) = 0.366 \text{ mol H}_2$$

$$-0.03769 x + 0.5348 = 0.366 \quad \text{from which } x = 4.48 \text{ g Fe}$$

2.36 a) $\text{NH}_3 + \text{CH}_4 \rightarrow \text{HCN} + 3 \text{H}_2$

b) The reaction system contains 700.0 g at the start, distributed as follows

$$\frac{500.0 \text{ g CH}_4}{16.043 \text{ g mol}^{-1}} = 31.17 \text{ mol CH}_4 \quad \text{and} \quad \frac{200.0 \text{ g NH}_3}{17.031 \text{ g mol}^{-1}} = 11.74 \text{ mol NH}_3$$

NH_3 is the limiting reactant. After the reaction goes to completion the system contains

$$m_{\text{HCN}} = 11.74 \text{ mol NH}_3 \times \frac{1 \text{ mol HCN}}{1 \text{ mol NH}_3} \times \frac{27.026 \text{ g}}{\text{mol HCN}} = 317.3 \text{ g HCN}$$

$$m_{\text{H}_2} = 11.74 \text{ mol NH}_3 \times \frac{3 \text{ mol H}_2}{1 \text{ mol NH}_3} \times \frac{2.0158 \text{ g}}{\text{mol H}_2} = 71.0 \text{ g H}_2$$

$$m_{\text{CH}_4} = (31.17 - 11.74 \text{ mol CH}_4) \times \frac{16.043 \text{ g}}{\text{mol CH}_4} = 311.7 \text{ g CH}_4$$

The sum of these three masses is 700.0 g, the same total mass as before the reaction.

2.38 The theoretical yield of TiCl_4 is

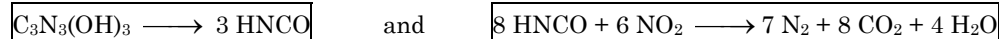
$$m_{\text{TiCl}_4} = 7.39 \text{ kg TiO}_2 \times \frac{1 \text{ kmol TiO}_2}{79.88 \text{ kg TiO}_2} \times \frac{1 \text{ kmol TiCl}_4}{1 \text{ kmol TiCl}_2} \times \frac{189.69 \text{ kg TiCl}_4}{1 \text{ kmol TiCl}_4} = 17.55 \text{ kg}$$

The percentage yield is $14.24 \text{ kg}/17.55 \text{ kg} \times 100\% = 81.1\%$.

2.40 Do the calculations to five significant figures, the precision of the tabulated atomic mass of tungsten. There is 0.43134 mol of W in a 100.000 g sample of the white oxide, and 1.29395 mol of O. The ratio of these numbers is 2.9998—the empirical formula is WO_3 . 100.000 g of the blue oxide contains 0.43975 mol W and 1.19709 mol of O. The ratio of these two amounts is 2.7222. This turns out to equal the ratio of 49 to 18, within the precision of the data. Hence the formula $\text{W}_{18}\text{O}_{49}$ is a correct answer. The blue oxide is really a nonstoichiometric compound, however.

2.42 Consider a 100.00 g sample of this binary compound. It contains 78.06 g of Ni and 21.94 g of O. This is $78.06 \text{ g}/58.69 \text{ g mol}^{-1} = 1.330 \text{ mol}$ of Ni and $21.94 \text{ g}/15.9994 \text{ g mol}^{-1} = 1.371 \text{ mol}$ of O. The ratio of these two chemical amounts is 1.031 to 1. If the data are truly precise to four significant figures, the compound is almost certainly a nonstoichiometric compound. The “almost” appears because “ $\text{Ni}_{1000}\text{O}_{1031}$ ” is a conceivable stoichiometric formulation. These subscripts are whole numbers, but they are hardly small whole numbers.

- 2.44 a) The balanced equations for the conversion of cyanuric acid to isocyanuric acid and the reaction of isocyanuric acid with nitrogen dioxide are



Balancing by inspection in the second equation works but requires some care. Assign 1 as the coefficient of HNCO. Then, focus on C and H because these elements occur in only one compound on each side of the equation. If HNCO on the left has a coefficient of 1, CO₂ on the right must have a coefficient of 1 and H₂O on the right must have a coefficient of $\frac{1}{2}$ to achieve balance in C and H. These two coefficients on the right imply a total of $2\frac{1}{2}$ mol of O on the right. The "1 HNCO" on the left supplies only 1 mol of O, and its coefficient must not be changed. The NO₂ must supply the other $\frac{3}{2}$ mol of O. To do this, its coefficient must be $\frac{3}{4}$. The left side now has $1 + \frac{3}{4} = \frac{7}{4}$ mol of N. The coefficient of N₂ on the right must therefore equal $\frac{7}{8}$ because $\frac{7}{8} \times 2 = \frac{7}{4}$ (the 2 comes from the subscript in N₂). Multiplying all five coefficients by 8 eliminates fractional coefficients.

b) Use a series of unit-factors constructed from the molar masses of the compounds and the coefficients of the two balanced equations

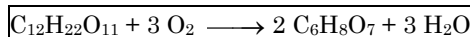
- 2.46 The only product of the reaction that contains nitrogen is m-toluidine; the only reactant that contains nitrogen is 3'-methylphthalanilic acid. It follows that the mass of nitrogen in the 3'-methylphthalanilic acid must equal the mass of nitrogen in the m-toluidine. The m-toluidine (empirical formula C₇H₉N) is 13.1% nitrogen by mass (calculated as in problem 2.1). The 5.23 g of m-toluidine therefore contains 0.685 g of nitrogen. The 3'-methylphthalanilic acid contains 5.49% nitrogen by mass (as given in the problem). The issue thus becomes finding the mass of 3'-methylphthalanilic acid that contains 0.685 g of nitrogen. Let this mass equal x . Then $0.0549x = 0.685$ g. Solving gives x equal to 12.5 g. This analysis is equivalent to the following:

$$m = 5.23 \text{ g toluidine} \times \left(\frac{13.1 \text{ g N}}{100 \text{ g toluidine}} \right) \left(\frac{100 \text{ g 3'-methyl...}}{5.49 \text{ g N}} \right) = \boxed{12.5 \text{ g 3'-methyl...}}$$

- 2.48 a) Write an unbalanced equation to represent what the statement of the problem reveals about the process



Balance this equation as to carbon by inserting the coefficient 2 in front of the citric acid. Then balance the H atoms by putting a 3 in front of the water (of the 22 H's on the left, 16 appear in the citric acid, and the rest appear in the water). Next, consider the oxygen. The right side has $(2 \times 7) + (3 \times 1) = 17$ O's. On the left side, the sucrose furnishes 11 O's so the remaining 6 must come from 3 molecules of oxygen. The balanced equation is



b) The balanced equation provides the information to write the second unit-factor in the following

$$\begin{aligned} m_{\text{C}_6\text{H}_8\text{O}_7} &= 15.0 \text{ kg sucrose} \times \left(\frac{1 \text{ kmol sucrose}}{342.3 \text{ kg sucrose}} \right) \left(\frac{2 \text{ kmol citric acid}}{1 \text{ kmol sucrose}} \right) \left(\frac{192.12 \text{ kg citric acid}}{1 \text{ kmol citric acid}} \right) \\ &= \boxed{16.8 \text{ kg citric acid}} \end{aligned}$$

Tip. Save some effort by creating and using unit-factors such as "1 kilomole sucrose / 342.3 kg sucrose." Also, only *part* of the balanced equation is needed, namely the 2 : 1 molar ratio of citric acid to sucrose. The O₂ and H₂O could have been left out.

- 2.50 a) Compute the number of moles of XBr_2 that is present and recognize that two moles of AgBr appear for every one mole of XBr_2 present in the 5.000 g sample. This fact appears in the second unit-factor in the following

$$n_{\text{XBr}_2} = 1.0198 \text{ g AgBr} \times \left(\frac{1 \text{ mol AgBr}}{187.77 \text{ g AgBr}} \right) \left(\frac{1 \text{ mol XBr}_2}{2 \text{ mol AgBr}} \right) = 0.002716 \text{ mol XBr}_2$$

The molar mass M of any substance equals its mass divided by its chemical amount

$$M_{\text{XBr}_2} = \frac{m_{\text{XBr}_2}}{n_{\text{XBr}_2}} = \frac{0.5000 \text{ g}}{0.002716 \text{ mol}} = 184.1 \text{ g mol}^{-1}$$

- b) The relative atomic mass of element X equals the relative molecular mass of the compound minus the contribution of the bromine:

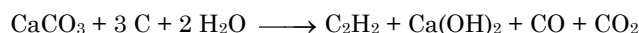
$$\text{relative atomic mass of X} = 184.1 - 2(79.9) = \boxed{24.3}$$

Checking the atomic masses in the periodic table shows that X is magnesium, $\boxed{\text{Mg}}$.

- 2.52 In step 1 of the Solvay process, 1 mol of NH_3 (along with 1 mol of H_2O) combines with 1 mol of CO_2 , holding it for attack by NaCl . This attack (step 2) gives 1 mol of NaHCO_3 while driving off NH_4Cl as a by-product. Heating the 1 mol of NaHCO_3 (step 3) then gives $\frac{1}{2}$ mol of the product Na_2CO_3 . For each mole of NH_3 that is put in, $\frac{1}{2}$ mol of Na_2CO_3 comes out. The following set-up uses this fact. It also uses the fact that a metric ton (1000 kg) is a megagram (1 Mg, a million grams) and the fact that a megamole (Mmol) is 10^6 (one million) moles.

$$m_{\text{Na}_2\text{CO}_3} = 1 \text{ metric ton NH}_3 \times \left(\frac{1 \text{ Mg}}{1 \text{ metric ton}} \right) \left(\frac{1 \text{ Mmol NH}_3}{17.03 \text{ Mg NH}_3} \right) \left(\frac{1/2 \text{ Mmol Na}_2\text{CO}_3}{1 \text{ Mmol NH}_3} \right) \\ \times \left(\frac{105.99 \text{ Mg Na}_2\text{CO}_3}{1 \text{ Mmol Na}_2\text{CO}_3} \right) \left(\frac{1 \text{ metric ton}}{1 \text{ Mg}} \right) = \boxed{3.11 \text{ metric ton Na}_2\text{CO}_3}$$

- 2.54 Assume that the limestone raw material is pure calcium carbonate (CaCO_3). Add the three steps listed in the problem. The CaO cancels out between the first and second steps and the CaC_2 cancels out between the second and third. The result



is balanced. It indicates that the over-all process generates 1 mol of C_2H_2 for every 1 mol of CaCO_3 that is put in. Use this fact as a unit-factor to obtain the theoretical yield of (C_2H_2) (acetylene). It is not necessary to compute the theoretical yields of CaO (lime) and CaC_2 (calcium carbide) formed and subsequently consumed on the way to the final product. The following set-up uses two additional facts: a metric ton is 10^6 g, also called a megagram (Mg), and a megamole (Mmol) is 10^6 moles.

$$m_{\text{C}_2\text{H}_2} = 10.0 \text{ Mg CaCO}_3 \times \left(\frac{1 \text{ Mmol CaCO}_3}{100.1 \text{ Mg CaCO}_3} \right) \left(\frac{1 \text{ Mmol C}_2\text{H}_2}{1 \text{ Mmol CaCO}_3} \right) \left(\frac{26.03 \text{ Mg C}_2\text{H}_2}{1 \text{ Mmol C}_2\text{H}_2} \right) \\ = 2.60 \text{ Mg C}_2\text{H}_2$$

The percent yield equals the actual yield divided by the theoretical yield and multiplied by 100%:

$$\text{percent yield C}_2\text{H}_2 = \frac{2.32 \text{ Mg C}_2\text{H}_2}{2.60 \text{ Mg C}_2\text{H}_2} \times 100\% = 89.2\%$$

Tip. "Overall" (sum of steps) chemical equations sometimes fool people. The one used here provides a correct molar relationship between the CaCO_3 and C_2H_2 . It does *not* indicate that CaCO_3 reacts directly with C and H_2O .