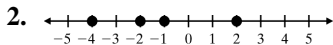


## Chapter 2

### Section 2.1 Practice Exercises

1. a. If 0 represents the surface of the earth, then 3805 below the surface of the earth is  $-3805$ .
- b. If zero degrees Fahrenheit is represented by  $0^{\circ}\text{F}$ , then 85 degrees below zero, Fahrenheit is represented by  $-85^{\circ}\text{F}$ .



3. a.  $0 > -5$  since 0 is to the right of  $-5$  on a number line.
- b.  $-3 < 3$  since  $-3$  is to the left of 3 on a number line.
- c.  $-7 > -12$  since  $-7$  is to the right of  $-12$  on a number line.
4. a.  $|-6| = 6$  because  $-6$  is 6 units from 0.
- b.  $|4| = 4$  because 4 is 4 units from 0.
- c.  $|-12| = 12$  because  $-12$  is 12 units from 0.
5. a. The opposite of 14 is  $-14$ .
- b. The opposite of  $-9$  is  $-(-9)$  or 9.
6. a.  $-|-7| = -7$
- b.  $-|4| = -4$
- c.  $-(-12) = 12$
7.  $-|x| = -|-6| = -6$
8. The planet with the highest average daytime surface temperature is the one that corresponds to the bar that extends the furthest in the positive direction (upward). Venus has the highest average daytime surface temperature.

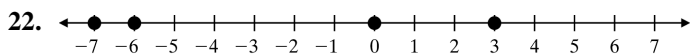
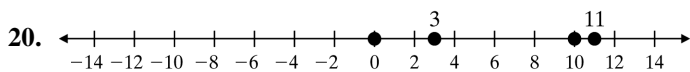
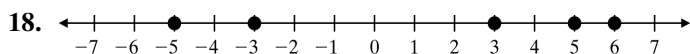
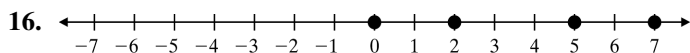
### Vocabulary, Readiness & Video Check 2.1

1. The numbers  $\dots-3, -2, -1, 0, 1, 2, 3, \dots$  are called integers.
2. Positive numbers, negative numbers, and zero together are called signed numbers.
3. The symbols " $<$ " and " $>$ " are called inequality symbols.
4. Numbers greater than 0 are called positive numbers while numbers less than 0 are called negative numbers.
5. The sign " $<$ " means is less than and " $>$ " means is greater than.
6. On a number line, the greater number is to the right of the lesser number.
7. A number's distance from 0 on the number line is the number's absolute value.
8. The numbers  $-5$  and 5 are called opposites.

9. number of feet a miner works underground
10. The tick marks are labeled with the integers.
11. 0 will always be greater than any of the negative integers.
12. 8;  $|8| = 8$  also.
13. A negative sign can be translated into the phrase "opposite of."
14. Eyre

## Exercise Set 2.1

2. If 0 represents the surface of the water, then 25 feet below the surface of the water is  $-25$ .
4. If 0 represents sea level, then 282 feet below sea level is  $-282$ .
6. If 0 represents 0 degrees Fahrenheit, then 134 degrees above zero is  $+134$ .
8. If 0 represents the surface of the ocean, then 14,040 below the surface of the ocean is  $-14,040$ .
10. If 0 represents a loss of \$0, then a loss of \$555 million is  $-555$  million.
12. If 0 represents  $0^\circ$  Celsius, then  $10^\circ$  below  $0^\circ$  Celsius is  $-10$ . Since  $5^\circ$  below  $0^\circ$  Celsius is  $-5$  and  $-10$  is less than  $-5$ ,  $-10$  (or  $10^\circ$  below  $0^\circ$  Celsius) is cooler.
14. If 0 represents a decrease of 0%, then a 23 percent decrease is  $-23$ .

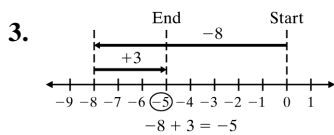
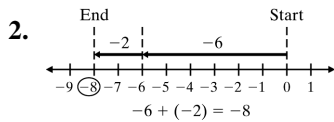
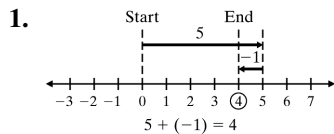


24.  $-8 < 0$  since  $-8$  is to the left of 0 on a number line.
26.  $-12 < -10$  since  $-12$  is to the left of  $-10$  on a number line.
28.  $-27 > -29$  since  $-27$  is to the right of  $-29$  on a number line.
30.  $13 > -13$  since 13 is to the right of  $-13$  on a number line.
32.  $|7| = 7$  since 7 is 7 units from 0 on a number line.
34.  $|-19| = 19$  since  $-19$  is 19 units from 0 on a number line.
36.  $|100| = 100$  since 100 is 100 units from 0 on a number line.
38.  $|-10| = 10$  since  $-10$  is 10 units from 0 on a number line.

40. The opposite of 8 is negative 8.  
 $-(8) = -8$
42. The opposite of negative 6 is 6.  
 $-(-6) = 6$
44. The opposite of 123 is negative 123.  
 $-(123) = -123$
46. The opposite of negative 13 is 13.  
 $-(-13) = 13$
48.  $|-11| = 11$
50.  $-|43| = -43$
52.  $-|-18| = -18$
54.  $-(-27) = 27$
56.  $-(-14) = 14$
58.  $-|-29| = -29$
60.  $-|x| = -|-8| = -8$
62.  $-|-x| = -|-10| = -10$
64.  $|x| = |32| = 32$
66.  $|-x| = |-1| = 1$
68.  $-4 > -17$  since  $-4$  is to the right of  $-17$  on a number line.
70.  $|-8| = 8$   
 $|-4| = 4$   
 Since  $8 > 4$ ,  $|-8| > |-4|$ .
72.  $-|17| = -17$   
 $-(-17) = 17$   
 Since  $-17 < 17$ ,  $-|17| < -(-17)$ .
74.  $|-24| = 24$   
 $-(-24) = 24$   
 Since  $24 = 24$ ,  $|-24| = -(-24)$ .
76.  $-45 < 0$  since  $-45$  is to the left of 0 on a number line.
78.  $|-45| = 45$   
 $|0| = 0$   
 Since  $45 > 0$ ,  $|-45| > |0|$ .
80.  $-|-8| = -8$   
 $-|-4| = -4$   
 Since  $-8 < -4$ ,  $-|-8| < -|-4|$ .
82.  $-(-38) = 38$   
 Since  $-22 < 38$ ,  $-22 < -(-38)$ .
84. If the number is  $-13$ , then the absolute value of  $-13$  is 13 and the opposite of  $-13$  is 13.
86. If the opposite of a number is 90, then the number is  $-90$  and its absolute value is 90.
88. The 'bar' that is equal to 0 corresponds to Lake Maracaibo, so Lake Maracaibo has an elevation at sea level.
90. The bar that extends second to the farthest in the negative direction corresponds to Lake Eyre, so Lake Eyre has the second lowest elevation.
92. The smallest number on the graph is  $-269^\circ\text{C}$ , which corresponds to helium.
94. The number on the graph closest to  $+300^\circ\text{C}$  is  $280^\circ\text{C}$ , which corresponds to phosphorus.
96.  $9 + 0 = 9$
98. 
$$\begin{array}{r} 20 \\ + 15 \\ \hline 35 \end{array}$$
100. 
$$\begin{array}{r} 1 \\ 362 \\ 37 \\ + 90 \\ \hline 489 \end{array}$$
102.  $|10| = 10$ ,  $2^3 = 8$ ,  $-|-5| = -5$ , and  $-(-4) = 4$ , so the numbers in order from least to greatest are  $-|-5|$ ,  $-(-4)$ ,  $2^3$ ,  $|10|$ .
104.  $1^4 = 1$ ,  $-(-3) = 3$ ,  $-|7| = -7$ , and  $|-20| = 20$ , so the numbers in order from least to greatest are  $-|7|$ ,  $1^4$ ,  $-(-3)$ ,  $|-20|$ .
106.  $3^3 = 27$ ,  $-|-11| = -11$ ,  $-(-10) = 10$ ,  $-4 = -4$ ,  $-|2| = -2$ , so the numbers in order from least to greatest are  $-|-11|$ ,  $-4$ ,  $-|2|$ ,  $-(-10)$ , and  $3^3$ .

108. a.  $|0| = 0$ ; since  $0 < 4$ , then  $|0| > 4$  is false.  
 b.  $|-4| = 4$ ; since  $4 = 4$ , then  $|-4| > 4$  is false.  
 c.  $|5| = 5$ ; since  $5 > 4$ , then  $|5| > 4$  is true.  
 d.  $|-100| = 100$ ; since  $100 > 4$ , then  $|-100| > 4$  is true.
110.  $(-|(-7)|) = (-|7|) = -7$
112. False; consider 0, where  $|0| = 0$  and 0 is not positive.
114. True; zero is always less than a positive number since it is to the left of it on a number line.
116. No;  $b > a$  because  $b$  is to the right of  $a$  on the number line.
118. answers may vary
120. no; answers may vary

Section 2.2 Practice Exercises



4.  $|-3| + |-19| = 3 + 19 = 22$   
 The common sign is negative, so  
 $(-3) + (-19) = -22$ .
5.  $-12 + (-30) = -42$
6.  $9 + 4 = 13$
7.  $|-1| = 1$ ,  $|26| = 26$ , and  $26 - 1 = 25$   
 $26 > 1$ , so the answer is positive.  
 $-1 + 26 = 25$
8.  $|2| = 2$ ,  $|-18| = 18$ , and  $18 - 2 = 16$   
 $18 > 2$ , so the answer is negative.  
 $2 + (-18) = -16$

9.  $-54 + 20 = -34$
10.  $7 + (-2) = 5$
11.  $-3 + 0 = -3$
12.  $18 + (-18) = 0$
13.  $-64 + 64 = 0$
14.  $6 + (-2) + (-15) = 4 + (-15) = -11$
15.  $5 + (-3) + 12 + (-14) = 2 + 12 + (-14)$   
 $= 14 + (-14)$   
 $= 0$
16.  $x + 3y = -6 + 3(2) = -6 + 6 = 0$
17.  $x + y = -13 + (-9) = -22$
18. Temperature at 8 a.m.  $= -7 + (+4) + (+7)$   
 $= -3 + (+7)$   
 $= 4$   
 The temperature was  $4^{\circ}\text{F}$  at 8 a.m.

Calculator Explorations

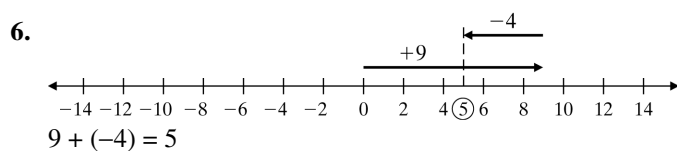
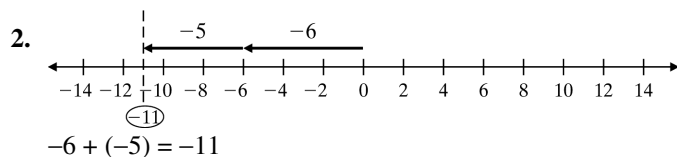
1.  $-256 + 97 = -159$
2.  $811 + (-1058) = -247$
3.  $6(15) + (-46) = 44$
4.  $-129 + 10(48) = 351$
5.  $-108,650 + (-786,205) = -894,855$
6.  $-196,662 + (-129,856) = -326,518$

Vocabulary, Readiness & Video Check 2.2

1. If  $n$  is a number, then  $-n + n = 0$ .
2. Since  $x + n = n + x$ , we say that addition is commutative.
3. If  $a$  is a number, then  $-(-a) = a$ .
4. Since  $n + (x + a) = (n + x) + a$ , we say that addition is associative.
5. Negative; the numbers have different signs and the sign of the sum is the same as the sign of the number with the larger absolute value,  $-6$ .

6. Negative; the numbers have the same sign—both are negative—and we keep this common sign in the sum.
7. The diver's current depth is 231 feet below the surface.

## Exercise Set 2.2



8.  $15 + 42 = 57$
10.  $|-5| + |-4| = 5 + 4 = 9$   
The common sign is negative, so  $-5 + (-4) = -9$ .
12.  $-62 + 62 = 0$
14.  $|8| - |-3| = 8 - 3 = 5$   
 $8 > 3$ , so the answer is positive.  
 $8 + (-3) = 5$
16.  $-8 + 0 = -8$
18.  $|-9| - |5| = 9 - 5 = 4$   
 $9 > 5$ , so the answer is negative.  
 $5 + (-9) = -4$
20.  $|-6| + |-1| = 6 + 1 = 7$   
The common sign is negative, so  $-6 + (-1) = -7$ .
22.  $|-23| + |-23| = 23 + 23 = 46$   
The common sign is negative, so  $-23 + (-23) = -46$ .
24.  $|-400| + |-256| = 400 + 256 = 656$   
The common sign is negative, so  $-400 + (-256) = -656$ .
26.  $|24| - |-10| = 24 - 10 = 14$   
 $24 > 10$ , so the answer is positive.  
 $24 + (-10) = 14$

28.  $|-8| - |4| = 8 - 4 = 4$   
 $8 > 4$ , so the answer is negative.  
 $-8 + 4 = -4$
30.  $|-89| - |37| = 89 - 37 = 52$   
 $89 > 37$ , so the answer is negative.  
 $-89 + 37 = -52$
32.  $|62| - |-32| = 62 - 32 = 30$   
 $62 > 32$ , so the answer is positive.  
 $-32 + 62 = 30$
34.  $|-375| - |325| = 375 - 325 = 50$   
 $375 > 325$ , so the answer is negative.  
 $325 + (-375) = -50$
36.  $|-56| + |-33| = 56 + 33 = 89$   
The common sign is negative, so  
 $-56 + (-33) = -89$ .
38.  $-1 + 5 + (-8) = 4 + (-8) = -4$
40.  $-103 + (-32) + (-27) = -135 + (-27) = -162$
42.  $18 + (-9) + 5 + (-2) = 9 + 5 + (-2)$   
 $= 14 + (-2)$   
 $= 12$
44.  $34 + (-12) + (-11) + 213 = 22 + (-11) + 213$   
 $= 11 + 213$   
 $= 224$
46.  $-12 + (-3) + (-5) = -15 + (-5) = -20$
48.  $-35 + (-12) = -47$
50.  $3 + (-23) + 6 = -20 + 6 = -14$
52.  $-100 + 70 = -30$
54.  $(-45) + 22 + 20 = -23 + 20 = -3$
56.  $-87 + 0 = -87$
58.  $-16 + 6 + (-14) + (-20) = -10 + (-14) + (-20)$   
 $= -24 + (-20)$   
 $= -44$
60.  $x + y = -1 + (-29) = -30$
62.  $3x + y = 3(7) + (-11) = 21 + (-11) = 10$
64.  $3x + y = 3(13) + (-17) = 39 + (-17) = 22$
66. The sum of  $-30$  and  $15$  is  $-30 + 15 = -15$ .
68. The sum of  $-49$ ,  $-2$ , and  $40$  is  
 $-49 + (-2) + 40 = -51 + 40 = -11$ .
70.  $0 + (-248) + 8 + (-16) + (-28) + 32$   
 $= -248 + 8 + (-16) + (-28) + 32$   
 $= -240 + (-16) + (-28) + 32$   
 $= -256 + (-28) + 32$   
 $= -284 + 32$   
 $= -252$   
The diver's final depth is 252 meters below the surface.
72. Since  $-7 < -2$ , Dufner won Round 2.
74. The bar for 2001 has a height of  $-25$ , so the net income in 2001 was  $-\$25,000,000$ .
76.  $3496 + 8240 + 25,922 = 37,658$   
The total net income for the years 2007, 2009, and 2011 was  $\$37,658,000,000$ .
78.  $14 + (-5) + (-8) + 7 = 9 + (-8) + 7 = 1 + 7 = 8$   
Her total score was 8.
80.  $-10,412 + (-1786) + 15,395 + 31,418$   
 $= -12,198 + 15,395 + 31,418$   
 $= 3197 + 31,418$   
 $= 34,615$   
The net income for all the years shown is  $\$34,615$ .
82.  $-45 + 3 = -42$   
Pennsylvania's all-time record low temperature is  $-42^\circ\text{F}$ .
84.  $-10,924 + 3245 = -7679$   
The depth of the Aleutian Trench is  $-7679$  meters.
86.  $91 - 0 = 91$
88.  $400$   
 $- 18$   
 $\hline 382$
90. answers may vary
92.  $-4 + 14 = 10$
94.  $-15 + (-17) = -32$
96. True
98. True

100. answers may vary

### Section 2.3 Practice Exercises

- $13 - 4 = 13 + (-4) = 9$
- $-8 - 2 = -8 + (-2) = -10$
- $11 - (-15) = 11 + 15 = 26$
- $-9 - (-1) = -9 + 1 = -8$
- $6 - 9 = 6 + (-9) = -3$
- $-14 - 5 = -14 + (-5) = -19$
- $-3 - (-4) = -3 + 4 = 1$
- $-15 - 6 = -15 + (-6) = -21$
- $-6 - 5 - 2 - (-3) = -6 + (-5) + (-2) + 3$   
 $= -11 + (-2) + 3$   
 $= -13 + 3$   
 $= -10$
- $8 + (-2) - 9 - (-7) = 8 + (-2) + (-9) + 7$   
 $= 6 + (-9) + 7$   
 $= -3 + 7$   
 $= 4$
- $x - y = -5 - 13 = -5 + (-13) = -18$
- $3y - z = 3(9) - (-4) = 27 + 4 = 31$
- $29,028 - (-1312) = 29,028 + 1312 = 30,340$   
 Mount Everest is 30,340 feet higher than the Dead Sea.

### Vocabulary, Readiness & Video Check 2.3

- It is true that  $a - b = \underline{a + (-b)}$ . b
- The opposite of  $n$  is  $\underline{-n}$ . a
- To evaluate  $x - y$  for  $x = -10$  and  $y = -14$ , we replace  $x$  with  $-10$  and  $y$  with  $-14$  and evaluate  $\underline{-10 - (-14)}$ . d
- The expression  $-5 - 10$  equals  $\underline{-5 + (-10)}$ . c
- additive inverse
- $-3 + 4 + (23) + (-10)$ ; all the subtraction operations are rewritten as additions in one step rather than changing one operation at a time as you work from left to right.

7. to follow the order of operations

8. The warmest temperature is  $265^\circ\text{F}$  warmer than the coldest temperature.

### Exercise Set 2.3

- $-6 - (-6) = -6 + 6 = 0$
- $15 - 12 = 15 + (-12) = 3$
- $2 - 5 = 2 + (-5) = -3$
- $12 - (-12) = 12 + 12 = 24$
- $-25 - (-25) = -25 + 25 = 0$
- $-2 - 42 = -2 + (-42) = -44$
- $8 - 9 = 8 + (-9) = -1$
- $17 - 63 = 17 + (-63) = -46$
- $844 - (-20) = 844 + 20 = 864$
- $-5 - 8 = -5 + (-8) = -13$
- $-12 - (-5) = -12 + 5 = -7$
- $16 - 45 = 16 + (-45) = -29$
- $-22 - 10 = -22 + (-10) = -32$
- $-8 - (-13) = -8 + 13 = 5$
- $-50 - (-50) = -50 + 50 = 0$
- $-35 + (-11) = -46$
- $4 - 21 = 4 + (-21) = -17$
- $-105 - 68 = -105 + (-68) = -173$
- $86 - 98 = 86 + (-98) = -12$
- $8 - 4 - 1 = 8 + (-4) + (-1) = 4 + (-1) = 3$
- $30 - 18 - 12 = 30 + (-18) + (-12)$   
 $= 12 + (-12)$   
 $= 0$
- $-10 - 6 - (-9) = -10 + (-6) + 9 = -16 + 9 = -7$
- $-15 + (-8) - 4 = -15 + (-8) + (-4)$   
 $= -23 + (-4)$   
 $= -27$

48.  $23 - (-17) + (-9) = 23 + 17 + (-9)$   
 $= 40 + (-9)$   
 $= 31$
50.  $-(-9) - 14 + (-23) = 9 + (-14) + (-23)$   
 $= -5 + (-23)$   
 $= -28$
52.  $-6 - (-8) + (-12) - 7 = -6 + 8 + (-12) + (-7)$   
 $= 2 + (-12) + (-7)$   
 $= -10 + (-7)$   
 $= -17$
54.  $5 + (-18) - (-21) - 2 = 5 + (-18) + 21 + (-2)$   
 $= -13 + 21 + (-2)$   
 $= 8 + (-2)$   
 $= 6$
56.  $x - y = -7 - 1 = -7 + (-1) = -8$
58.  $x - y = 9 - (-2) = 9 + 2 = 11$
60.  $2x - y = 2(8) - (-10) = 16 + 10 = 26$
62.  $2x - y = 2(14) - (-12) = 28 + 12 = 40$
64. The temperature in November is  $3^{\circ}\text{F}$  and in December is  $-4^{\circ}\text{F}$ .  
 $3 - (-4) = 3 + 4 = 7$   
The difference is  $7^{\circ}\text{F}$ .
66. The month with the warmest temperature is July,  $63^{\circ}\text{F}$ , and the month with the coldest temperature is January,  $-8^{\circ}\text{F}$ .  
 $63 - (-8) = 63 + 8 = 71$   
The difference is  $71^{\circ}\text{F}$ .
68.  $134 - (-80) = 134 + 80 = 214$   
Therefore,  $134^{\circ}\text{F}$  is  $214^{\circ}\text{F}$  warmer than  $-80^{\circ}\text{F}$ .
70.  $93 - 18 - 26 = 93 + (-18) + (-26)$   
 $= 75 + (-26)$   
 $= 49$   
She owes \$49 on her account.
72.  $13,796 - (-21,857) = 13,796 + 21,857 = 35,653$   
The difference in elevation is 35,653 feet.
74.  $-384 - (-505) = -384 + 505 = 121$   
The difference in elevation is 121 feet.
76.  $-236 - (-505) = -236 + 505 = 269$   
The difference in elevation is 269 feet.
78.  $512 - (-92) = 512 + 92 = 604$   
The difference in elevation is 604 feet.
80.  $-52 - (-92) = -52 + 92 = 40$   
The difference in elevation is 40 feet.
82.  $845 - (-162) = 845 + 162 = 1007$   
The difference in temperature is  $1007^{\circ}\text{F}$ .
84.  $1165 - 3878 = 1165 + (-3878) = -2713$   
The trade balance was  $-2713$  million barrels.
86. The difference of  $-3$  and a number is  $-3 - x$ .
88. Add a number and  $-36$  is  $x + (-36)$ .
90.  $\frac{96}{3} = 32$
- $$\begin{array}{r} 32 \\ 3 \overline{) 96} \\ \underline{-96} \\ 0 \end{array}$$
92.  $\begin{array}{r} 51 \\ \times 89 \\ \hline 459 \\ 4080 \\ \hline 4539 \end{array}$
94. answers may vary
96.  $-4 - 8 = -4 + (-8) = -12$
98.  $-3 - (-10) = -3 + 10 = 7$
100.  $|-12| - |-5| = 12 - 5 = 12 + (-5) = 7$
102.  $|-8| - |8| = 8 - 8 = 0$
104.  $|-23| - |-42| = 23 - 42 = 23 + (-42) = -19$
106.  $|-2 - (-6)| = |-2 + 6| = |4| = 4$   
 $|-2| - |-6| = 2 - 6 = 2 + (-6) = -4$   
Since  $4 \neq -4$ , the statement is false.
108. no; answers may vary

## Section 2.4 Practice Exercises

1.  $-3 \cdot 8 = -24$
2.  $-5(-2) = 10$



3.  $0 \cdot (-20) = 0$
4.  $10(-5) = -50$
5.  $8(-6)(-2) = -48(-2) = 96$
6.  $(-9)(-2)(-1) = 18(-1) = -18$
7.  $(-3)(-4)(-5)(-1) = 12(-5)(-1) = -60(-1) = 60$
8.  $(-2)^4 = (-2)(-2)(-2)(-2)$   
 $= 4(-2)(-2)$   
 $= -8(-2)$   
 $= 16$
9.  $-8^2 = -(8 \cdot 8) = -64$
10.  $\frac{42}{-7} = -6$
11.  $-16 \div (-2) = 8$
12.  $\frac{-80}{10} = -8$
13.  $\frac{-6}{0}$  is undefined.
14.  $\frac{0}{-7} = 0$
15.  $xy = 5 \cdot (-8) = -40$
16.  $\frac{x}{y} = \frac{-12}{-3} = 4$
17. total score =  $4 \cdot (-13) = -52$   
 The card player's total score was  $-52$ .

**Vocabulary, Readiness & Video Check 2.4**

1. The product of a negative number and a positive number is a negative number.
2. The product of two negative numbers is a positive number.
3. The quotient of two negative numbers is a positive number.
4. The quotient of a negative number and a positive number is a negative number.

5. The product of a negative number and zero is 0.
6. The quotient of 0 and a negative number is 0.
7. The quotient of a negative number and 0 is undefined.
8. When a negative sign is involved in an expression with an exponent, parentheses tell you whether or not the exponent applies to the negative sign. In Example 3,  $(-3)^2$ , the exponent applies to everything within the parentheses, so  $-3$  is squared; in Example 4,  $-3^2$ , the exponent does *not* apply to the sign and only 3 is squared.
9. We can find out about sign rules for division because we know sign rules for multiplication.
10. That  $ab$  means  $a \cdot b$ .
11. The phrase "lost four yards" in the example translates to the negative number  $-4$ .

**Exercise Set 2.4**

2.  $5(-3) = -15$
4.  $-7(-2) = 14$
6.  $-9(7) = -63$
8.  $-6(0) = 0$
10.  $-2(3)(-7) = -6(-7) = 42$
12.  $-8(-3)(-3) = 24(-3) = -72$
14.  $2(-5)(-4) = -10(-4) = 40$
16.  $3(0)(-4)(-8) = 0$
18.  $-2(-1)(3)(-2) = 2(3)(-2) = 6(-2) = -12$
20.  $-2^4 = -(2)(2)(2)(2) = -4(2)(2) = -8(2) = -16$
22.  $(-1)^4 = (-1)(-1)(-1)(-1)$   
 $= 1(-1)(-1)$   
 $= -1(-1)$   
 $= 1$
24.  $-4^3 = -(4 \cdot 4 \cdot 4) = -64$

26.  $(-3)^2 = (-3)(-3) = 9$

28.  $90 \div (-9) = -10$

30.  $\frac{56}{-8} = -7$

32.  $\frac{-32}{4} = -8$

34.  $\frac{-13}{0}$  is undefined.

36.  $\frac{0}{-15} = 0$

38.  $\frac{-24}{-12} = 2$

40.  $0(-100) = 0$

42.  $-6 \cdot 2 = -12$

44.  $-12(13) = -156$

46.  $-9(-5) = 45$

48.  $-7(-5)(-3) = 35(-3) = -105$

50.  $(-5)^2 = (-5)(-5) = 25$

52.  $-\frac{30}{5} = -6$

54.  $-\frac{49}{7} = -7$

56.  $-15 \div 3 = -5$

58.  $6(-5)(-2) = -30(-2) = 60$

60.  $-20 \cdot 5 \cdot (-5) \cdot (-3) = -100 \cdot (-5) \cdot (-3)$   
 $= 500 \cdot (-3)$   
 $= -1500$

62.  $\frac{0}{-14} = 0$

64.  $\frac{63}{-9} = -7$

66.  $480 \div (-8) = \frac{480}{-8} = -60$

68.  $\frac{-36}{-3} = 12$

70.  $-2^3 = -(2 \cdot 2 \cdot 2) = -8$

72.  $(-11)^2 = (-11)(-11) = 121$

74.  $-1(2)(7)(-3) = -2(7)(-3) = -14(-3) = 42$

76.  $(-1)^{33} = -1$ , since there are an odd number of factors.

78.  $-2(-2)(-3)(-2) = 4(-3)(-2) = -12(-2) = 24$

80. 
$$\begin{array}{r} 56 \\ \times 43 \\ \hline 168 \\ 2240 \\ \hline 2408 \\ -56 \cdot 43 = -2408 \end{array}$$

82. 
$$\begin{array}{r} 23 \\ \times 70 \\ \hline 1610 \\ 70 \cdot (-23) = -1610 \end{array}$$

84.  $ab = 5(-1) = -5$

86.  $ab = (-8)(8) = -64$

88.  $ab = (-9)(-6) = 54$

90.  $\frac{x}{y} = \frac{9}{-3} = -3$

92.  $\frac{x}{y} = \frac{0}{-5} = 0$

94.  $\frac{x}{y} = \frac{-10}{-10} = 1$

96.  $xy = 20 \cdot (-5) = -100$   
 $\frac{x}{y} = \frac{20}{-5} = -4$

98.  $xy = -3 \cdot 0 = 0$

$\frac{x}{y} = \frac{-3}{0}$  is undefined.

100.  $-63 \div (-3) = 21$

The quotient of  $-63$  and  $-3$  is  $21$ .

102.  $49$

$$\begin{array}{r} \times 5 \\ \hline 245 \end{array}$$

$-49(5) = -245$

The product of  $-49$  and  $5$  is  $-245$ .

104. The quotient of  $-8$  and a number is  $\frac{-8}{x}$  or

$-8 \div x$ .

106. The sum of a number and  $-12$  is  $x + (-12)$ .

108. The difference of a number and  $-10$  is  $x - (-10)$ .

110. Multiply a number by  $-17$  is  $x \cdot (-17)$  or  $-17x$ .

112. A loss of  $\$400$  is represented by  $-400$ .

$7 \cdot (-400) = -2800$

His total loss was  $\$2800$ .

114. A drop of  $5$  degrees is represented by  $-5$ .

$6 \cdot (-5) = -30$

The total drop in temperature was  $30$  degrees.

116.  $-1 \cdot (-39) = 39$

The melting point of rubidium is  $39^\circ\text{C}$ .

118.  $-11 \cdot (-70) = 770$

The melting point of strontium is  $770^\circ\text{C}$ .

120.  $\frac{-30,000}{3} = -10,000$

The expected loss for each month would be  $10,000$  shipments or  $-10,000$  shipments per month.

122. a.  $405 - 30 = 375$

There were about  $375$  more California Condors in  $2012$  than in  $1987$ . This is a change of  $375$  condors.

b. This is a period of  $25$  years.

$$\frac{375}{25} = 15 \qquad \begin{array}{r} 15 \\ 25 \overline{) 375} \\ \underline{-25} \phantom{0} \\ 125 \\ \underline{-125} \\ 0 \end{array}$$

The average change was  $15$  California Condors per year.

124.  $3 \cdot (7 - 4) + 2 \cdot 5^2 = 3 \cdot 3 + 2 \cdot 5^2$   
 $= 3 \cdot 3 + 2 \cdot 25$   
 $= 9 + 2 \cdot 25$   
 $= 9 + 50$   
 $= 59$

126.  $12 \div (4 - 2) + 7 = 12 \div 2 + 7 = 6 + 7 = 13$

128.  $-9(-11) = 99$

130.  $-4 + (-3) + 21 = -7 + 21 = 14$

132.  $-16 - (-2) = -16 + 2 = -14$

134. The product of an even number of negative numbers is positive, so the product of ten negative numbers is positive.

136.  $(-1)^{50}$  and  $(-7)^{20}$  are positive since there are an even number of factors. Note that  $(-7)^{20} > (-1)^{50}$  since  $(-1)^{50} = 1$ .

$(-1)^{55}$  and  $(-7)^{23}$  are negative since there are an odd number of factors. Note that  $(-7)^{23} < (-1)^{55}$  since  $(-1)^{55} = -1$ .

$0^{15} = 0$

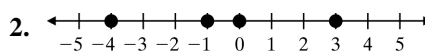
The numbers from least to greatest are

$(-7)^{23}$ ,  $(-1)^{55}$ ,  $0^{15}$ ,  $(-1)^{50}$ ,  $(-7)^{20}$ .

138. answers may vary

### Integrated Review

1. Let  $0$  represent  $0^\circ\text{F}$ . Then  $50$  degrees below zero is represented by  $-50$  and  $122$  degrees above zero is represented by  $+122$  or  $122$ .



3.  $0 > -10$  since  $0$  is to the right of  $-10$  on a number line.

4.  $-4 < 4$  since  $-4$  is to the left of  $4$  on a number line.
5.  $-15 < -5$  since  $-15$  is to the left of  $-5$  on a number line.
6.  $-2 > -7$  since  $-2$  is to the right of  $-7$  on a number line.
7.  $|-3| = 3$  because  $-3$  is 3 units from 0.
8.  $|-9| = 9$  because  $-9$  is 9 units from 0.
9.  $-|-4| = -4$
10.  $-(-5) = 5$
11. The opposite of 11 is  $-11$ .
12. The opposite of  $-3$  is  $-(-3) = 3$ .
13. The opposite of 64 is  $-64$ .
14. The opposite of 0 is  $-0 = 0$ .
15.  $-3 + 15 = 12$
16.  $-9 + (-11) = -20$
17.  $-8(-6)(-1) = 48(-1) = -48$
18.  $-18 \div 2 = -9$
19.  $65 + (-55) = 10$
20.  $1000 - 1002 = 1000 + (-1002) = -2$
21.  $53 - (-53) = 53 + 53 = 106$
22.  $-2 - 1 = -2 + (-1) = -3$
23.  $\frac{0}{-47} = 0$
24.  $\frac{-36}{-9} = 4$
25.  $-17 - (-59) = -17 + 59 = 42$
26.  $-8 + (-6) + 20 = -14 + 20 = 6$
27.  $\frac{-95}{-5} = 19$
28.  $-9(100) = -900$
29.  $-12 - 6 - (-6) = -12 + (-6) + 6 = -18 + 6 = -12$
30.  $-4 + (-8) - 16 - (-9) = -4 + (-8) + (-16) + 9$   
 $= -12 + (-16) + 9$   
 $= -28 + 9$   
 $= -19$
31.  $\frac{-105}{0}$  is undefined.
32.  $7(-16)(0)(-3) = 0$  (since one factor is 0)
33. Subtract  $-8$  from  $-12$  is  
 $-12 - (-8) = -12 + 8 = -4$ .
34. The sum of  $-17$  and  $-27$  is  $-17 + (-27) = -44$ .
35. The product of  $-5$  and  $-25$  is  $-5(-25) = 125$ .
36. The quotient of  $-100$  and  $-5$  is  $\frac{-100}{-5} = 20$ .
37. Divide a number by  $-17$  is  $\frac{x}{-17}$  or  $x \div (-17)$ .
38. The sum of  $-3$  and a number is  $-3 + x$ .
39. A number decreased by  $-18$  is  $x - (-18)$ .
40. The product of  $-7$  and a number is  $-7 \cdot x$  or  $-7x$ .
41.  $x + y = -3 + 12 = 9$
42.  $x - y = -3 - 12 = -3 + (-12) = -15$
43.  $2y - x = 2(12) - (-3) = 24 - (-3) = 24 + 3 = 27$
44.  $3y + x = 3(12) + (-3) = 36 + (-3) = 33$
45.  $5x = 5(-3) = -15$
46.  $\frac{y}{x} = \frac{12}{-3} = -4$

## Section 2.5 Practice Exercises

1.  $(-2)^4 = (-2)(-2)(-2)(-2) = 16$
2.  $-2^4 = -(2)(2)(2)(2) = -16$
3.  $3 \cdot 6^2 = 3 \cdot (6 \cdot 6) = 3 \cdot 36 = 108$

$$4. \frac{-25}{5(-1)} = \frac{-25}{-5} = 5$$

$$5. \frac{-18+6}{-3-1} = \frac{-12}{-4} = 3$$

$$6. \begin{aligned} 30+50+(-4)^3 &= 30+50+(-64) \\ &= 80+(-64) \\ &= 16 \end{aligned}$$

$$7. -2^3 + (-4)^2 + 1^5 = -8+16+1 = 8+1 = 9$$

$$8. \begin{aligned} 2(2-9)+(-12)-3 &= 2(-7)+(-12)-3 \\ &= -14+(-12)-3 \\ &= -26-3 \\ &= -29 \end{aligned}$$

$$9. \begin{aligned} (-5) \cdot |-8| + (-3) + 2^3 &= (-5) \cdot 8 + (-3) + 2^3 \\ &= (-5) \cdot 8 + (-3) + 8 \\ &= -40 + (-3) + 8 \\ &= -43 + 8 \\ &= -35 \end{aligned}$$

$$10. \begin{aligned} -4[-6+5(-3+5)]-7 &= -4[-6+5(2)]-7 \\ &= -4[-6+10]-7 \\ &= -4(4)-7 \\ &= -16-7 \\ &= -23 \end{aligned}$$

$$11. \begin{aligned} x^2 &= (-15)^2 = (-15)(-15) = 225 \\ -x^2 &= -(-15)^2 = -(-15)(-15) = -225 \end{aligned}$$

$$12. \begin{aligned} 5y^2 &= 5(4)^2 = 5(16) = 80 \\ 5y^2 &= 5(-4)^2 = 5(16) = 80 \end{aligned}$$

$$13. x^2 + y = (-6)^2 + (-3) = 36 + (-3) = 33$$

$$14. 4 - x^2 = 4 - (-8)^2 = 4 - 64 = -60$$

$$15. \begin{aligned} \text{average} &= \frac{\text{sum of numbers}}{\text{number of numbers}} \\ &= \frac{17+(-1)+(-11)+(-13)+(-16)+(-13)+2}{7} \\ &= \frac{-35}{7} \\ &= -5 \end{aligned}$$

The average of the temperatures is  $-5^\circ\text{F}$ .

### Calculator Explorations

$$1. \frac{-120-360}{-10} = 48$$

$$2. \frac{4750}{-2+(-17)} = -250$$

$$3. \frac{-316+(-458)}{28+(-25)} = -258$$

$$4. \frac{-234+86}{-18+16} = 74$$

### Vocabulary, Readiness & Video Check 2.5

- To simplify  $-2 \div 2 \cdot (3)$  which operation should be performed first? division
- To simplify  $-9 - 3 \cdot 4$ , which operation should be performed first? multiplication
- The average of a list of numbers is  $\frac{\text{sum of numbers}}{\text{number of numbers}}$ .
- To simplify  $5[-9 + (-3)] \div 4$ , which operation should be performed first? addition
- To simplify  $-2 + 3(10 - 12) \cdot (-8)$ , which operation should be performed first? subtraction
- To evaluate  $x - 3y$  for  $x = -7$  and  $y = -1$ , replace  $x$  with  $-7$  and  $y$  with  $-1$  and evaluate  $-7 - 3(-1)$ .
- A fraction bar means divided by and it is a grouping symbol.
- To make sure that the entire value of  $-2$ , including the sign, is squared.
- Finding the average is a good application of both order of operations and adding and dividing integers.

### Exercise Set 2.5

$$2. -2^4 = -(2)(2)(2)(2) = -16$$

$$4. (-2)^4 = (-2)(-2)(-2)(-2) = 16$$

$$6. 5 \cdot 2^3 = 5 \cdot 8 = 40$$

8.  $10 - 23 - 12 = -13 - 12 = -25$
10.  $-8 + 4(3) = -8 + 12 = 4$
12.  $7(-6) + 3 = -42 + 3 = -39$
14.  $-12 + 6 \div 3 = -12 + 2 = -10$
16.  $5 + 9 \cdot 4 - 20 = 5 + 36 - 20$   
 $= 41 - 20$   
 $= 21$
18.  $\frac{20-15}{-1} = \frac{5}{-1} = -5$
20.  $\frac{88}{-8-3} = \frac{88}{-11} = -8$
22.  $7(-4) - (-6) = -28 + 6 = -22$
24.  $[9 + (-2)]^3 = [7]^3 = 343$
26.  $7 \cdot 6 - 6 \cdot 5 + (-10) = 42 - 6 \cdot 5 + (-10)$   
 $= 42 - 30 + (-10)$   
 $= 12 + (-10)$   
 $= 2$
28.  $7 - (-5)^2 = 7 - 25 = -18$
30.  $|-3 + 7| \cdot 7^2 = |4| \cdot 7^2 = 4 \cdot 7^2 = 4 \cdot 49 = 196$
32.  $10 \cdot 5^3 + 7 = 10 \cdot 125 + 7 = 1250 + 7 = 1257$
34.  $8^2 - (5-2)^4 = 8^2 - 3^4 = 64 - 81 = -17$
36.  $|12 - 19| \div 7 = |-7| \div 7 = 7 \div 7 = 1$
38.  $-(-2)^3 = -(-8) = 8$
40.  $(2-7)^2 \div (4-3)^4 = (-5)^2 \div 1^4 = 25 \div 1 = 25$
42.  $|3-15| \cdot (-4) \div (-16) = |-12| \cdot (-4) \div (-16)$   
 $= 12 \cdot (-4) \div (-16)$   
 $= -48 \div (-16)$   
 $= 3$
44.  $(-20-5) \div 5 - 15 = (-25) \div 5 - 15 = -5 - 15 = -20$
46.  $3 \cdot (8-3) + (-4) - 10 = 3 \cdot (5) + (-4) - 10$   
 $= 15 + (-4) - 10$   
 $= 11 - 10$   
 $= 1$
48.  $(4-12) \cdot (8-17) = (-8) \cdot (-9) = 72$
50.  $(-4 \div 4) - (8 \div 8) = (-1) - (1) = -2$
52.  $(11-3^2)^3 = (11-9)^3 = 2^3 = 8$
54.  $-3(4-8)^2 + 5(14-16)^3 = -3(-4)^2 + 5(-2)^3$   
 $= -3(16) + 5(-8)$   
 $= -48 + (-40)$   
 $= -88$
56.  $12 - [7 - (3-6)] + (2-3)^3$   
 $= 12 - [7 - (-3)] + (2-3)^3$   
 $= 12 - (7+3) + (-1)^3$   
 $= 12 - 10 + (-1)$   
 $= 2 + (-1)$   
 $= 1$
58.  $\frac{10(-1) - (-2)(-3)}{2[-8 \div (-2-2)]} = \frac{-10-6}{2[-8 \div (-4)]}$   
 $= \frac{-16}{2(2)}$   
 $= \frac{-16}{4}$   
 $= -4$
60.  $-2[6 + 4(2-8)] - 25 = -2[6 + 4(-6)] - 25$   
 $= -2[6 + (-24)] - 25$   
 $= -2(-18) - 25$   
 $= 36 - 25$   
 $= 11$
62.  $x - y - z = -2 - 4 - (-1)$   
 $= -2 - 4 + 1$   
 $= -6 + 1$   
 $= -5$
64.  $5x - y + 4z = 5(-2) - 4 + 4(-1)$   
 $= -10 - 4 + (-4)$   
 $= -14 + (-4)$   
 $= -18$
66.  $x^2 + z = (-2)^2 + (-1) = 4 + (-1) = 3$

$$68. \frac{4x}{y} = \frac{4(-2)}{4} = \frac{-8}{4} = -2$$

$$70. z^2 = (-4)^2 = 16$$

$$72. -x^2 = -(-3)^2 = -9$$

$$74. 3x^2 = 3(-3)^2 = 3(9) = 27$$

$$76. 3 - z^2 = 3 - (-4)^2 = 3 - 16 = -13$$

$$78. 3z^2 - x = 3(-4)^2 - (-3) = 3(16) + 3 = 48 + 3 = 51$$

$$80. \text{average} = \frac{-18 + (-8) + (-1) + (-1) + 0 + 4}{6}$$

$$= \frac{-24}{6}$$

$$= -4$$

$$82. \text{average} = \frac{-40 + (-20) + (-10) + (-15) + (-5)}{5}$$

$$= \frac{-90}{5}$$

$$= -18$$

84. The two lowest scores are  $-12$  and  $-5$ .  
 $-5 - (-12) = -5 + 12 = 7$   
 The difference between the two lowest scores is 7.

$$86. \text{average} = \frac{-12 + (-5) + (-1) + 6}{4} = \frac{-12}{4} = -3$$

The average of the scores is  $-3$ .

88. no; answers may vary

$$90. 90 \div 45 = 2$$

$$92. 45 + 90 = 135$$

94.  $3 + 5 + 3 + 5 = 16$   
 The perimeter is 16 centimeters.

96.  $17 + 23 + 32 = 72$   
 The perimeter is 72 meters.

$$98. (7 \cdot 3 - 4) \cdot 2 = (21 - 4) \cdot 2 = 17 \cdot 2 = 34$$

$$100. 2 \cdot (8 \div 4 - 20) = 2 \cdot (2 - 20) = 2 \cdot (-18) = -36$$

102. answers may vary

104. answers may vary

$$106. (-17)^6 = (-17)(-17)(-17)(-17)(-17)(-17)$$

$$= 24,137,569$$

$$108. 3x^2 + 2x - y = 3(-18)^2 + 2(-18) - 2868$$

$$= 3(324) + (-36) - 2868$$

$$= 972 + (-36) - 2868$$

$$= 936 - 2868$$

$$= -1932$$

$$110. 5(ab + 3)^b = 5(-2 \cdot 3 + 3)^3$$

$$= 5(-6 + 3)^3$$

$$= 5(-3)^3$$

$$= 5(-27)$$

$$= -135$$

### Section 2.6 Practice Exercises

$$1. \quad -4x - 3 = 5$$

$$-4(-2) - 3 \stackrel{?}{=} 5$$

$$8 - 3 \stackrel{?}{=} 5$$

$$5 = 5 \quad \text{True}$$

Since  $5 = 5$  is true,  $-2$  is a solution of the equation.

$$2. \quad y - 6 = -2$$

$$y - 6 + 6 = -2 + 6$$

$$y = 4$$

Check:  $y - 6 = -2$

$$4 - 6 \stackrel{?}{=} -2$$

$$-2 = -2 \quad \text{True}$$

The solution is 4.

$$3. \quad -2 = z + 8$$

$$-2 - 8 = z + 8 - 8$$

$$-10 = z$$

Check:  $-2 = z + 8$

$$-2 \stackrel{?}{=} -10 + 8$$

$$-2 = -2 \quad \text{True}$$

The solution is  $-10$ .

$$4. \quad x = -2 + 90 + (-100)$$

$$x = 88 + (-100)$$

$$x = -12$$

The solution is  $-12$ .

5.  $3y = -18$

$$\frac{3y}{3} = \frac{-18}{3}$$

$$\frac{3}{3} \cdot y = \frac{-18}{3}$$

$$y = -6$$

Check:  $3y = -18$

$$3(-6) \stackrel{?}{=} -18$$

$$-18 = -18 \quad \text{True}$$

The solution is  $-6$ .

6.  $-32 = 8x$

$$\frac{-32}{8} = \frac{8x}{8}$$

$$\frac{-32}{8} = \frac{8}{8} \cdot x$$

$$-4 = x$$

Check:  $-32 = 8x$

$$-32 \stackrel{?}{=} 8(-4)$$

$$-32 = -32 \quad \text{True}$$

The solution is  $-4$ .

7.  $-3y = -27$

$$\frac{-3y}{-3} = \frac{-27}{-3}$$

$$\frac{-3}{-3} \cdot y = \frac{-27}{-3}$$

$$y = 9$$

Check:  $-3y = -27$

$$-3 \cdot 9 \stackrel{?}{=} -27$$

$$-27 = -27 \quad \text{True}$$

The solution is  $9$ .

8.  $\frac{x}{-4} = 7$

$$-4 \cdot \frac{x}{-4} = -4 \cdot 7$$

$$\frac{-4}{-4} \cdot x = -4 \cdot 7$$

$$x = -28$$

Check:  $\frac{x}{-4} = 7$

$$\frac{-28}{-4} \stackrel{?}{=} 7$$

$$7 = 7 \quad \text{True}$$

The solution is  $-28$ .**Vocabulary, Readiness & Video Check 2.6**

1. A combination of operations on variables and numbers is called an expression.

2. A statement of the form

"expression = expression" is called an equation.

3. An equation contains an equal sign (=) while an expression does not.

4. An expression may be simplified and evaluated while an equation may be solved.

5. A solution of an equation is a number that when substituted for a variable makes the equation a true statement.

6. Equivalent equations have the same solution.

7. By the addition property of equality, the same number may be added to or subtracted from both sides of an equation without changing the solution of the equation.

8. By the multiplication property of equality, both sides of an equation may be multiplied or divided by the same nonzero number without changing the solution of the equation.

9. an equal sign

10. We can add the same number to both sides of an equation and we'll have an equivalent equation. Also, we can subtract the same number from both sides of an equation and have an equivalent equation.

11. To check a solution, we go back to the original equation, replace the variable with the proposed solution, and see if we get a true statement.

**Exercise Set 2.6**

2.  $y - 16 = -7$

$$9 - 16 \stackrel{?}{=} -7$$

$$-7 = -7 \quad \text{True}$$

Since  $-7 = -7$  is true,  $9$  is a solution of the equation.

4.  $a + 23 = -16$

$$-7 + 23 \stackrel{?}{=} -16$$

$$16 = -16 \quad \text{False}$$

Since  $16 = -16$  is false,  $-7$  is not a solution of the equation.



6.  $-3k = 12 - k$   
 $-3(-6) \stackrel{?}{=} 12 - (-6)$   
 $18 \stackrel{?}{=} 12 + 6$   
 $18 = 18$  True  
 Since  $18 = 18$  is true,  $-6$  is a solution of the equation.

8.  $2(b - 3) = 10$   
 $2(1 - 3) \stackrel{?}{=} 10$   
 $2(-2) \stackrel{?}{=} 10$   
 $-4 = 10$  False  
 Since  $-4 = 10$  is false,  $1$  is not a solution of the equation.

10.  $f + 4 = -6$   
 $f + 4 - 4 = -6 - 4$   
 $f = -10$   
 Check:  $f + 4 = -6$   
 $-10 + 4 \stackrel{?}{=} -6$   
 $-6 = -6$  True  
 The solution is  $-10$ .

12.  $s - 7 = -15$   
 $s - 7 + 7 = -15 + 7$   
 $s = -8$   
 Check:  $s - 7 = -15$   
 $-8 - 7 \stackrel{?}{=} -15$   
 $-15 = -15$  True  
 The solution is  $-8$ .

14.  $1 = y + 7$   
 $1 - 7 = y + 7 - 7$   
 $-6 = y$   
 Check:  $1 = y + 7$   
 $1 \stackrel{?}{=} -6 + 7$   
 $1 = 1$  True  
 The solution is  $-6$ .

16.  $-50 + 40 - 5 = z$   
 $-10 - 5 = z$   
 $-15 = z$   
 Check:  $-50 + 40 - 5 = z$   
 $-50 + 40 - 5 \stackrel{?}{=} -15$   
 $-10 - 5 \stackrel{?}{=} -15$   
 $-15 = -15$  True  
 The solution is  $-15$ .

18.  $6y = 48$   
 $\frac{6y}{6} = \frac{48}{6}$   
 $y = 8$   
 Check:  $6y = 48$   
 $6(8) \stackrel{?}{=} 48$   
 $48 = 48$  True  
 The solution is  $8$ .

20.  $-2x = 26$   
 $\frac{-2x}{-2} = \frac{26}{-2}$   
 $x = -13$   
 Check:  $-2x = 26$   
 $-2(-13) \stackrel{?}{=} 26$   
 $26 = 26$  True  
 The solution is  $-13$ .

22.  $\frac{n}{11} = -5$   
 $11 \cdot \frac{n}{11} = 11 \cdot (-5)$   
 $n = -55$   
 Check:  $\frac{n}{11} = -5$   
 $\frac{-55}{11} \stackrel{?}{=} -5$   
 $-5 = -5$  True  
 The solution is  $-55$ .

24.  $7y = -21$   
 $\frac{7y}{7} = \frac{-21}{7}$   
 $y = -3$   
 Check:  $7y = -21$   
 $7 \cdot (-3) \stackrel{?}{=} -21$   
 $-21 = -21$  True  
 The solution is  $-3$ .

$$\begin{aligned}
 26. \quad & -9x = 0 \\
 & \frac{-9x}{-9} = \frac{0}{-9} \\
 & \frac{-9}{-9} \cdot x = \frac{0}{-9} \\
 & x = 0 \\
 \text{Check: } & -9x = 0 \\
 & -9 \cdot 0 \stackrel{?}{=} 0 \\
 & 0 = 0 \quad \text{True} \\
 & \text{The solution is 0.}
 \end{aligned}$$

$$\begin{aligned}
 28. \quad & -31x = -31 \\
 & \frac{-31x}{-31} = \frac{-31}{-31} \\
 & \frac{-31}{-31} \cdot x = \frac{-31}{-31} \\
 & x = 1 \\
 \text{Check: } & -31x = -31 \\
 & -31 \cdot 1 \stackrel{?}{=} -31 \\
 & -31 = -31 \quad \text{True} \\
 & \text{The solution is 1.}
 \end{aligned}$$

$$\begin{aligned}
 30. \quad & 3y = -27 \\
 & \frac{3y}{3} = \frac{-27}{3} \\
 & \frac{3}{3} \cdot y = \frac{-27}{3} \\
 & y = -9 \\
 & \text{The solution is } -9.
 \end{aligned}$$

$$\begin{aligned}
 32. \quad & n - 4 = -48 \\
 & n - 4 + 4 = -48 + 4 \\
 & n = -44 \\
 & \text{The solution is } -44.
 \end{aligned}$$

$$\begin{aligned}
 34. \quad & -36 = y + 12 \\
 & -36 - 12 = y + 12 - 12 \\
 & -48 = y \\
 & \text{The solution is } -48.
 \end{aligned}$$

$$\begin{aligned}
 36. \quad & \frac{x}{-9} = -9 \\
 & -9 \cdot \frac{x}{-9} = -9 \cdot (-9) \\
 & \frac{-9}{-9} \cdot x = -9 \cdot (-9) \\
 & x = 81 \\
 & \text{The solution is 81.}
 \end{aligned}$$

$$\begin{aligned}
 38. \quad & z = -28 + 36 \\
 & z = 8 \\
 & \text{The solution is 8.}
 \end{aligned}$$

$$\begin{aligned}
 40. \quad & -11x = -121 \\
 & \frac{-11x}{-11} = \frac{-121}{-11} \\
 & \frac{-11}{-11} \cdot x = \frac{-121}{-11} \\
 & x = 11 \\
 & \text{The solution is 11.}
 \end{aligned}$$

$$\begin{aligned}
 42. \quad & \frac{n}{5} = -20 \\
 & 5 \cdot \frac{n}{5} = 5 \cdot (-20) \\
 & \frac{5}{5} \cdot n = 5 \cdot (-20) \\
 & n = -100 \\
 & \text{The solution is } -100.
 \end{aligned}$$

$$\begin{aligned}
 44. \quad & -81 = 27x \\
 & \frac{-81}{27} = \frac{27x}{27} \\
 & \frac{-81}{27} = \frac{27}{27} \cdot x \\
 & -3 = x \\
 & \text{The solution is } -3.
 \end{aligned}$$

46. A number increased by  $-5$  is  $x + (-5)$ .

48. The quotient of a number and  $-20$  is  $x \div (-20)$  or  $\frac{x}{-20}$ .

50.  $-32$  multiplied by a number is  $-32 \cdot x$  or  $-32x$ .

52. Subtract a number from  $-18$  is  $-18 - x$ .

$$\begin{aligned}
 54. \quad & n + 961 = 120 \\
 & n + 961 - 961 = 120 - 961 \\
 & n = -841 \\
 & \text{The solution is } -841.
 \end{aligned}$$

$$\begin{aligned}
 56. \quad & \frac{y}{-18} = 1098 \\
 & -18 \cdot \frac{y}{-18} = -18 \cdot 1098 \\
 & \frac{-18}{-18} \cdot y = -18 \cdot 1098 \\
 & y = -19,764 \\
 & \text{The solution is } -19,764.
 \end{aligned}$$

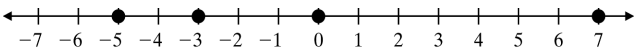

58. answers may vary

60. answers may vary

## Chapter 2 Vocabulary Check

- Two numbers that are the same distance from 0 on the number line but are on opposite sides of 0 are called opposites.
- The absolute value of a number is that number's distance from 0 on a number line.
- The integers are ..., -3, -2, -1, 0, 1, 2, 3, ....
- The negative numbers are numbers less than zero.
- The positive numbers are numbers greater than zero.
- The symbols “<” and “>” are called inequality symbols.
- A solution of an equation is a number that when substituted for a variable makes the equation a true statement.
- The average of a list of numbers is  $\frac{\text{sum of numbers}}{\text{number of numbers}}$ .
- A combination of operations on variables and numbers is called an expression.
- A statement of the form “expression = expression” is called an equation.
- The sign “<” means is less than and “>” means is greater than.
- By the addition property of equality, the same number may be added to or subtracted from both sides of an equation without changing the solution of the equation.
- By the multiplication property of equality, both sides of an equation may be multiplied or divided by the same nonzero number without changing the solution of the equation.

## Chapter 2 Review

- If 0 represents ground level, then 1572 feet below the ground is  $-1572$ .
- If 0 represents sea level, then an elevation of 11,239 feet is  $+11,239$ .
- A number line from -7 to 7 with tick marks at every integer. Dots are placed at -5, -3, 0, and 7.
- A number line from -7 to 7 with tick marks at every integer. Dots are placed at -6, -1, 0, and 5.
- $|-11| = 11$  since  $-11$  is 11 units from 0 on a number line.
- $|0| = 0$  since 0 is 0 units from 0 on a number line.
- $-|8| = -8$
- $-(-9) = 9$
- $-|-16| = -16$
- $-(-2) = 2$
- $-18 > -20$  since  $-18$  is to the right of  $-20$  on a number line.

12.  $-5 < 5$  since  $-5$  is to the left of  $5$  on a number line.
13.  $|-123| = 123$   
 $-|-198| = -198$   
 Since  $123 > -198$ ,  $|-123| > -|-198|$ .
14.  $|-12| = 12$   
 $-|-16| = -16$   
 Since  $12 > -16$ ,  $|-12| > -|-16|$ .
15. The opposite of  $-18$  is  $18$ .  
 $-(-18) = 18$
16. The opposite of  $42$  is negative  $42$ .  
 $-(42) = -42$
17. False; consider  $a = 1$  and  $b = 2$ , then  $1 < 2$ .
18. True
19. True
20. True
21.  $|y| = |-2| = 2$
22.  $|-x| = |-(-3)| = |3| = 3$
23.  $-|-z| = -|-(-5)| = -|5| = -5$
24.  $-|-n| = -|-(-10)| = -|10| = -10$
25. The bar that extends the farthest in the negative direction corresponds to Elevator D, so Elevator D extends the farthest below ground.
26. The bar that extends the farthest in the positive direction corresponds to Elevator B, so Elevator B extends the highest above ground.
27.  $|5| - |-3| = 5 - 3 = 2$   
 $5 > 3$ , so the answer is positive.  
 $5 + (-3) = 2$
28.  $|18| - |-4| = 18 - 4 = 14$   
 $18 > 4$ , so the answer is positive.  
 $18 + (-4) = 14$
29.  $|16| - |-12| = 16 - 12 = 4$   
 $16 > 12$ , so the answer is positive.  
 $-12 + 16 = 4$
30.  $|40| - |-23| = 40 - 23 = 17$   
 $40 > 23$ , so the answer is positive.  
 $-23 + 40 = 17$
31.  $|-8| + |-15| = 8 + 15 = 23$   
 The common sign is negative, so  
 $-8 + (-15) = -23$ .
32.  $|-5| + |-17| = 5 + 17 = 22$   
 The common sign is negative, so  
 $-5 + (-17) = -22$ .
33.  $|-24| - |3| = 24 - 3 = 21$   
 $24 > 3$ , so the answer is negative.  
 $-24 + 3 = -21$
34.  $|-89| - |19| = 89 - 19 = 70$   
 $89 > 19$ , so the answer is negative.  
 $-89 + 19 = -70$
35.  $15 + (-15) = 0$
36.  $-24 + 24 = 0$
37.  $|-43| + |-108| = 43 + 108 = 151$   
 The common sign is negative, so  
 $-43 + (-108) = -151$ .
38.  $|-100| + |-506| = 100 + 506 = 606$   
 The common sign is negative, so  
 $-100 + (-506) = -606$ .
39.  $-15 + (-5) = -20$   
 The temperature at 6 a.m. is  $-20^{\circ}\text{C}$ .
40.  $-127 + (-23) = -150$   
 The diver's current depth is  $-150$  feet.
41.  $-6 + (-9) + (-4) + (-2) = -15 + (-4) + (-2)$   
 $= -19 + (-2)$   
 $= -21$   
 His total score was  $-21$ .
42.  $16 - 4 = 16 + (-4) = 12$   
 The team's score was  $12$ .
43.  $12 - 4 = 12 + (-4) = 8$
44.  $-12 - 4 = -12 + (-4) = -16$
45.  $-7 - 17 = -7 + (-17) = -24$
46.  $7 - 17 = 7 + (-17) = -10$
47.  $7 - (-13) = 7 + 13 = 20$
48.  $-6 - (-14) = -6 + 14 = 8$
49.  $16 - 16 = 16 + (-16) = 0$

50.  $-16 - 16 = -16 + (-16) = -32$

51.  $-12 - (-12) = -12 + 12 = 0$

52.  $-5 - (-12) = -5 + 12 = 7$

53. 
$$\begin{aligned} -(-5) - 12 + (-3) &= 5 + (-12) + (-3) \\ &= -7 + (-3) \\ &= -10 \end{aligned}$$

54. 
$$\begin{aligned} -8 + (-12) - 10 - (-3) &= -8 + (-12) + (-10) + 3 \\ &= -20 + (-10) + 3 \\ &= -30 + 3 \\ &= -27 \end{aligned}$$

55.  $600 - (-92) = 600 + 92 = 692$   
The difference in elevations is 692 feet.

56. 
$$\begin{aligned} 142 - 125 + 43 - 85 &= 142 + (-125) + 43 + (-85) \\ &= 17 + 43 + (-85) \\ &= 60 + (-85) \\ &= -25 \end{aligned}$$

The balance in his account is  $-25$ .

57.  $85 - 99 = 85 + (-99) = -14$   
You are  $-14$  feet or 14 feet below ground at the end of the drop.

58.  $66 - (-16) = 66 + 16 = 82$   
The total length of the elevator shaft for Elevator C is 82 feet.

59. 
$$\begin{aligned} |-5| - |-6| &= 5 - 6 = 5 + (-6) = -1 \\ 5 - 6 &= 5 + (-6) = -1 \\ |-5| - |-6| &= 5 - 6 \text{ is true.} \end{aligned}$$

60. 
$$\begin{aligned} |-5 - (-6)| &= |-5 + 6| = |1| = 1 \\ 5 + 6 &= 11 \end{aligned}$$
  
Since  $1 \neq 11$ , the statement is false.

61.  $-3(-7) = 21$

62.  $-6(3) = -18$

63.  $-4(16) = -64$

64.  $-5(-12) = 60$

65.  $(-5)^2 = (-5)(-5) = 25$

66.  $(-1)^5 = (-1)(-1)(-1)(-1)(-1) = -1$

67.  $12(-3)(0) = 0$

68.  $-1(6)(2)(-2) = -6(2)(-2) = -12(-2) = 24$

69.  $-15 \div 3 = -5$

70.  $\frac{-24}{-8} = 3$

71.  $\frac{0}{-3} = 0$

72.  $\frac{-46}{0}$  is undefined.

73.  $\frac{100}{-5} = -20$

74.  $\frac{-72}{8} = -9$

75.  $\frac{-38}{-1} = 38$

76.  $\frac{45}{-9} = -5$

77. A loss of 5 yards is represented by  $-5$ .  
 $(-5)(2) = -10$   
The total loss is 10 yards.

78. A loss of \$50 is represented by  $-50$ .  
 $(-50)(4) = -200$   
The total loss is \$200.

79. A debt of \$1024 is represented by  $-1024$ .  
 $-1024 \div 4 = -256$   
Each payment is \$256.

80. A drop of 45 degrees is represented by  $-45$ .  
 $\frac{-45}{9} = -5$  or  $-45 \div 9 = -5$

The average drop each hour is  $5^\circ\text{F}$ .

81.  $(-7)^2 = (-7)(-7) = 49$

82.  $-7^2 = -(7 \cdot 7) = -49$

83.  $5 - 8 + 3 = -3 + 3 = 0$

84.  $-3 + 12 + (-7) - 10 = 9 + (-7) - 10 = 2 - 10 = -8$

85.  $-10 + 3 \cdot (-2) = -10 + (-6) = -16$

86.  $5 - 10 \cdot (-3) = 5 - (-30) = 5 + 30 = 35$

87.  $16 \div (-2) \cdot 4 = -8 \cdot 4 = -32$

88.  $-20 \div 5 \cdot 2 = -4 \cdot 2 = -8$

89.  $16 + (-3) \cdot 12 \div 4 = 16 + (-36) \div 4$   
 $= 16 + (-9)$   
 $= 7$

90.  $-12 + 10 \div (-5) = -12 + (-2) = -14$

91.  $4^3 - (8-3)^2 = 4^3 - (5)^2 = 64 - 25 = 39$

92.  $(-3)^3 - 90 = -27 - 90 = -117$

93.  $\frac{(-4)(-3) - (-2)(-1)}{-10 + 5} = \frac{12 - 2}{-5} = \frac{10}{-5} = -2$

94.  $\frac{4(12-18)}{-10 \div (-2-3)} = \frac{4(-6)}{-10 \div (-5)} = \frac{-24}{2} = -12$

95.  $\text{average} = \frac{-18 + 25 + (-30) + 7 + 0 + (-2)}{6}$   
 $= \frac{-18}{6}$   
 $= -3$

96.  $\text{average} = \frac{-45 + (-40) + (-30) + (-25)}{4}$   
 $= \frac{-140}{4}$   
 $= -35$

97.  $2x - y = 2(-2) - 1 = -4 - 1 = -5$

98.  $y^2 + x^2 = 1^2 + (-2)^2 = 1 + 4 = 5$

99.  $\frac{3x}{6} = \frac{3(-2)}{6} = \frac{-6}{6} = -1$

100.  $\frac{5y-x}{-y} = \frac{5(1) - (-2)}{-1} = \frac{5+2}{-1} = \frac{7}{-1} = -7$

101.  $2n - 6 = 16$   
 $2(-5) - 6 \stackrel{?}{=} 16$   
 $-10 - 6 \stackrel{?}{=} 16$   
 $-16 = 16$  False

Since  $-16 = 16$  is false,  $-5$  is not a solution of the equation.

102.  $2(c-8) = -20$   
 $2(-2-8) \stackrel{?}{=} -20$   
 $2(-10) \stackrel{?}{=} -20$   
 $-20 = -20$  True

Since  $-20 = -20$  is true,  $-2$  is a solution of the equation.

103.  $n - 7 = -20$   
 $n - 7 + 7 = -20 + 7$   
 $n = -13$

The solution is  $-13$ .

104.  $-5 = n + 15$   
 $-5 - 15 = n + 15 - 15$   
 $-20 = n$

The solution is  $-20$ .

105.  $10x = -30$   
 $\frac{10x}{10} = \frac{-30}{10}$   
 $\frac{10}{10} \cdot x = \frac{-30}{10}$   
 $x = -3$

The solution is  $-3$ .

106.  $-8x = 72$   
 $\frac{-8x}{-8} = \frac{72}{-8}$   
 $\frac{-8}{-8} \cdot x = \frac{72}{-8}$   
 $x = -9$

The solution is  $-9$ .

107.  $-20 + 7 = y$   
 $-13 = y$

The solution is  $-13$ .

108.  $x - 31 = -62$   
 $x - 31 + 31 = -62 + 31$   
 $x = -31$

The solution is  $-31$ .

109.  $\frac{n}{-4} = -11$   
 $-4 \cdot \frac{n}{-4} = -4 \cdot (-11)$   
 $\frac{-4}{-4} \cdot n = -4 \cdot (-11)$   
 $n = 44$

The solution is  $44$ .

$$110. \quad \frac{x}{-2} = 13$$

$$-2 \cdot \frac{x}{-2} = -2 \cdot 13$$

$$\frac{-2}{-2} \cdot x = -2 \cdot 13$$

$$x = -26$$

The solution is  $-26$ .

$$111. \quad n + 12 = -7$$

$$n + 12 - 12 = -7 - 12$$

$$n = -19$$

The solution is  $-19$ .

$$112. \quad n - 40 = -2$$

$$n - 40 + 40 = -2 + 40$$

$$n = 38$$

The solution is  $38$ .

$$113. \quad -36 = -6x$$

$$\frac{-36}{-6} = \frac{-6x}{-6}$$

$$\frac{-36}{-6} = \frac{-6}{-6} \cdot x$$

$$6 = x$$

The solution is  $6$ .

$$114. \quad -40 = 8y$$

$$\frac{-40}{8} = \frac{8y}{8}$$

$$\frac{-40}{8} = \frac{8}{8} \cdot y$$

$$-5 = y$$

The solution is  $-5$ .

$$115. \quad -6 + (-9) = -15$$

$$116. \quad -16 - 3 = -16 + (-3) = -19$$

$$117. \quad -4(-12) = 48$$

$$118. \quad \frac{84}{-4} = -21$$

$$119. \quad -76 - (-97) = -76 + 97 = 21$$

$$120. \quad -9 + 4 = -5$$

$$121. \quad -18 - 9 = -27$$

The temperature on Friday was  $-27^{\circ}\text{C}$ .

$$122. \quad -11 + 17 = 6$$

The temperature at noon on Tuesday was  $6^{\circ}\text{C}$ .

$$123. \quad 12,923 - (-195) = 12,923 + 195 = 13,118$$

The difference in elevations is  $13,118$  feet.

$$124. \quad -32 + 23 = -9$$

His financial situation can be represented by  $-9$ .

$$125. \quad (3-7)^2 \div (6-4)^3 = (-4)^2 \div (2)^3 = 16 \div 8 = 2$$

$$126. \quad \begin{aligned} 3(4+2) + (-6) - 3^2 &= 3(6) + (-6) - 3^2 \\ &= 3(6) + (-6) - 9 \\ &= 18 + (-6) - 9 \\ &= 12 - 9 \\ &= 3 \end{aligned}$$

$$127. \quad 2 - 4 \cdot 3 + 5 = 2 - 12 + 5 = -10 + 5 = -5$$

$$128. \quad 4 - 6 \cdot 5 + 1 = 4 - 30 + 1 = -26 + 1 = -25$$

$$129. \quad \frac{-|-14| - 6}{7 + 2(-3)} = \frac{-14 - 6}{7 + (-6)} = \frac{-20}{1} = -20$$

$$130. \quad \begin{aligned} 5(7-6)^3 - 4(2-3)^2 + 2^4 &= 5(1)^3 - 4(-1)^2 + 2^4 \\ &= 5(1) - 4(1) + 16 \\ &= 5 - 4 + 16 \\ &= 1 + 16 \\ &= 17 \end{aligned}$$

$$131. \quad n - 9 = -30$$

$$n - 9 + 9 = -30 + 9$$

$$n = -21$$

The solution is  $-21$ .

$$132. \quad n + 18 = 1$$

$$n + 18 - 18 = 1 - 18$$

$$n = -17$$

The solution is  $-17$ .

$$133. \quad -4x = -48$$

$$\frac{-4x}{-4} = \frac{-48}{-4}$$

$$\frac{-4}{-4} \cdot x = \frac{-48}{-4}$$

$$x = 12$$

The solution is  $12$ .

$$\begin{aligned}
 134. \quad 9x &= -81 \\
 \frac{9x}{9} &= \frac{-81}{9} \\
 \frac{9}{9} \cdot x &= \frac{-81}{9} \\
 x &= -9
 \end{aligned}$$

The solution is  $-9$ .

$$\begin{aligned}
 135. \quad \frac{n}{-2} &= 100 \\
 -2 \cdot \frac{n}{-2} &= -2 \cdot 100 \\
 \frac{-2}{-2} \cdot n &= -2 \cdot 100 \\
 n &= -200
 \end{aligned}$$

The solution is  $-200$ .

$$\begin{aligned}
 136. \quad \frac{y}{-1} &= -3 \\
 -1 \cdot \frac{y}{-1} &= -1(-3) \\
 \frac{-1}{-1} \cdot y &= -1 \cdot (-3) \\
 y &= 3
 \end{aligned}$$

The solution is  $3$ .

### Chapter 2 Test

- $-5 + 8 = 3$
- $18 - 24 = 18 + (-24) = -6$
- $5 \cdot (-20) = -100$
- $-16 \div (-4) = 4$
- $-18 + (-12) = -30$
- $-7 - (-19) = -7 + 19 = 12$
- $-5 \cdot (-13) = 65$
- $\frac{-25}{-5} = 5$
- $|-25| + (-13) = 25 + (-13) = 12$
- $14 - |-20| = 14 - 20 = 14 + (-20) = -6$
- $|5| \cdot |-10| = 5 \cdot 10 = 50$
- $\frac{|-10|}{-|-5|} = \frac{10}{-5} = -2$

$$13. \quad -8 + 9 \div (-3) = -8 + (-3) = -11$$

$$\begin{aligned}
 14. \quad -7 + (-32) - 12 + 5 &= -7 + (-32) + (-12) + 5 \\
 &= -39 + (-12) + 5 \\
 &= -51 + 5 \\
 &= -46
 \end{aligned}$$

$$\begin{aligned}
 15. \quad (-5)^3 - 24 \div (-3) &= -125 - 24 \div (-3) \\
 &= -125 - (-8) \\
 &= -125 + 8 \\
 &= -117
 \end{aligned}$$

$$16. \quad (5-9)^2 \cdot (8-2)^3 = (-4)^2 \cdot (6)^3 = 16 \cdot 216 = 3456$$

$$17. \quad -(-7)^2 \div 7 \cdot (-4) = -49 \div 7 \cdot (-4) = -7 \cdot (-4) = 28$$

$$\begin{aligned}
 18. \quad 3 - (8-2)^3 &= 3 - 6^3 \\
 &= 3 - 216 \\
 &= 3 + (-216) \\
 &= -213
 \end{aligned}$$

$$19. \quad \frac{4}{2} - \frac{8^2}{16} = \frac{4}{2} - \frac{64}{16} = 2 - 4 = 2 + (-4) = -2$$

$$20. \quad \frac{-3(-2)+12}{-1(-4-5)} = \frac{6+12}{-1(-9)} = \frac{18}{9} = 2$$

$$21. \quad \frac{|25-30|^2}{2(-6)+7} = \frac{|-5|^2}{-12+7} = \frac{(5)^2}{-5} = \frac{25}{-5} = -5$$

$$\begin{aligned}
 22. \quad 5(-8) - [6 - (2-4)] + (12-16)^2 \\
 &= 5(-8) - [6 - (-2)] + (12-16)^2 \\
 &= 5(-8) - (6+2) + (-4)^2 \\
 &= 5(-8) - 8 + (-4)^2 \\
 &= 5(-8) - 8 + 16 \\
 &= -40 - 8 + 16 \\
 &= -48 + 16 \\
 &= -32
 \end{aligned}$$

$$\begin{aligned}
 23. \quad 7x + 3y - 4z &= 7(0) + 3(-3) - 4(2) \\
 &= 0 + (-9) - 8 \\
 &= -9 - 8 \\
 &= -17
 \end{aligned}$$

$$24. \quad 10 - y^2 = 10 - (-3)^2 = 10 - 9 = 1$$

$$25. \quad \frac{3z}{2y} = \frac{3(2)}{2(-3)} = \frac{6}{-6} = -1$$



26. A descent of 22 feet is represented by  $-22$ .  
 $4(-22) = -88$   
 Mary is 88 feet below sea level.

27.  $129 + (-79) + (-40) + 35 = 50 + (-40) + 35$   
 $= 10 + 35$   
 $= 45$

His new balance can be represented by 45.

28. Subtract the elevation of the Romanche Gap from the elevation of Mt. Washington.

$$6288 - (-25,354) = 6288 + 25,354 = 31,642$$

The difference in elevations is 31,642 feet.

29. Subtract the depth of the lake from the elevation of the surface.

$$1495 - 5315 = 1495 + (-5315) = -3820$$

The deepest point of the lake is 3820 feet below sea level.

30.  $\text{average} = \frac{-12 + (-13) + 0 + 9}{4} = \frac{-16}{4} = -4$

31. a. The product of a number and 17 is  $17 \cdot x$  or  $17x$ .

b. A number subtracted from 20 is  $20 - x$ .

32.  $-9n = -45$

$$\frac{-9n}{-9} = \frac{-45}{-9}$$

$$\frac{-9}{-9} \cdot n = \frac{-45}{-9}$$

$$n = 5$$

The solution is 5.

33.  $\frac{n}{-7} = 4$

$$-7 \cdot \frac{n}{-7} = -7 \cdot 4$$

$$\frac{-7}{-7} \cdot n = -7 \cdot 4$$

$$n = -28$$

The solution is  $-28$ .

34.  $x - 16 = -36$

$$x - 16 + 16 = -36 + 16$$

$$x = -20$$

The solution is  $-20$ .

35.  $-20 + 8 + 8 = x$

$$-12 + 8 = x$$

$$-4 = x$$

The solution is  $-4$ .

### Cumulative Review Chapters 1–2

- The place value of 3 in 396,418 is hundred-thousands.
- The place value of 3 in 4308 is hundreds.
- The place value of 3 in 93,192 is thousands.
- The place value of 3 in 693,298 is thousands.
- The place value of 3 in 534,275,866 is ten-millions.
- The place value of 3 in 267,301,818 is hundred-thousands.
- $-7 < 7$  since  $-7$  is to the left of 7 on a number line.
  - $0 > -4$  since 0 is to the right of  $-4$  on a number line.
  - $-9 > -11$  since  $-9$  is to the right of  $-11$  on a number line.
- $12 > -4$  since 12 is to the right of  $-4$  on a number line.
  - $-13 > -31$  since  $-13$  is to the right of  $-31$  on a number line.
  - $-82 < 79$  since  $-82$  is to the left of 79 on a number line.
- $13 + 2 + 7 + 8 + 9 = (13 + 7) + (2 + 8) + 9$   
 $= 20 + 10 + 9$   
 $= 39$
- $11 + 3 + 9 + 16 = (11 + 9) + (3 + 16) = 20 + 19 = 39$

11.  $7826$

$$- 505$$

$$\hline 7321$$

Check:  $7321$

$$+ 505$$

$$\hline 7826$$

$$\begin{array}{r} 12. \quad 3285 \\ - 272 \\ \hline 3013 \end{array}$$

Check:  $\begin{array}{r} 3013 \\ + 272 \\ \hline 3285 \end{array}$

13. Subtract 7257 from the radius of Jupiter.

$$\begin{array}{r} 43,441 \\ - 7,257 \\ \hline 36,184 \end{array}$$

The radius of Saturn is 36,184 miles.

14. Subtract the cost of the camera from the amount in her account.

$$\begin{array}{r} 762 \\ - 237 \\ \hline 525 \end{array}$$

She will have \$525 left in her account after buying the camera.

15. To round 568 to the nearest ten, observe that the digit in the ones place is 8. Since this digit is at least 5, we add 1 to the digit in the tens place. The number 568 rounded to the nearest ten is 570.

16. To round 568 to the nearest hundred, observe that the digit in the tens place is 6. Since this digit is at least 5, we add 1 to the digit in the hundreds place. The number 568 rounded to the nearest hundred is 600.

17.  $\begin{array}{r} 4725 \text{ rounds to } 4700 \\ - 2879 \text{ rounds to } -2900 \\ \hline 1800 \end{array}$

18.  $\begin{array}{r} 8394 \text{ rounds to } 8000 \\ - 2913 \text{ rounds to } -3000 \\ \hline 5000 \end{array}$

19. a.  $5(6 + 5) = 5 \cdot 6 + 5 \cdot 5$   
 b.  $20(4 + 7) = 20 \cdot 4 + 20 \cdot 7$

c.  $2(7 + 9) = 2 \cdot 7 + 2 \cdot 9$

20. a.  $5(2 + 12) = 5 \cdot 2 + 5 \cdot 12$

b.  $9(3 + 6) = 9 \cdot 3 + 9 \cdot 6$

c.  $4(8 + 1) = 4 \cdot 8 + 4 \cdot 1$

$$\begin{array}{r} 21. \quad 631 \\ \times 125 \\ \hline 3155 \\ 12620 \\ \hline 63775 \\ \hline 78,875 \end{array}$$

$$\begin{array}{r} 22. \quad 299 \\ \times 104 \\ \hline 1196 \\ 29900 \\ \hline 31,096 \end{array}$$

23. a.  $42 \div 7 = 6$  because  $6 \cdot 7 = 42$ .

b.  $\frac{64}{8} = 8$  because  $8 \cdot 8 = 64$ .

c.  $3 \overline{)21}$  because  $7 \cdot 3 = 21$ .

24. a.  $\frac{35}{5} = 7$  because  $7 \cdot 5 = 35$ .

b.  $64 \div 8 = 8$  because  $8 \cdot 8 = 64$ .

c.  $4 \overline{)48}$  because  $12 \cdot 4 = 48$ .

$$\begin{array}{r} 25. \quad 5 \overline{)3705} \\ \underline{-35} \phantom{0} \\ 20 \\ \underline{-20} \\ 05 \\ \underline{-5} \\ 0 \end{array}$$

Check:  $\begin{array}{r} 741 \\ \times 5 \\ \hline 3705 \end{array}$

$$\begin{array}{r} 26. \quad 8 \overline{)3648} \\ \underline{-32} \phantom{0} \\ 44 \\ \underline{-40} \\ 48 \\ \underline{-48} \\ 0 \end{array}$$

Check: 456

$$\begin{array}{r} \times 8 \\ \hline 3648 \end{array}$$

27. number of cards = number of cards + number of friends  
for each person = 238 ÷ 19

$$\begin{array}{r} 12 \text{ R } 10 \\ 19 \overline{) 238} \\ \underline{-19} \phantom{0} \\ 48 \\ \underline{-38} \\ 10 \end{array}$$

Each friend will receive 12 cards. There will be 10 cards left over.

28. Cost of each ticket = total cost ÷ number of tickets  
= 324 ÷ 36

$$\begin{array}{r} 9 \\ 36 \overline{) 324} \\ \underline{-324} \\ 0 \end{array}$$

Each ticket cost \$9.

29.  $9^2 = 9 \cdot 9 = 81$

30.  $5^3 = 5 \cdot 5 \cdot 5 = 125$

31.  $6^1 = 6$

32.  $4^1 = 4$

33.  $5 \cdot 6^2 = 5 \cdot 6 \cdot 6 = 180$

34.  $2^3 \cdot 7 = 2 \cdot 2 \cdot 2 \cdot 7 = 56$

35.  $\frac{7-2 \cdot 3+3^2}{5(2-1)} = \frac{7-2 \cdot 3+9}{5(1)} = \frac{7-6+9}{5} = \frac{10}{5} = 2$

36.  $\frac{6^2+4 \cdot 4+2^3}{37-5^2} = \frac{36+4 \cdot 4+8}{37-25} = \frac{36+16+8}{12} = \frac{60}{12} = 5$

37.  $x + 6 = 8 + 6 = 14$

38.  $5 + x = 5 + 9 = 14$

39. a.  $|-9| = 9$  because  $-9$  is 9 units from 0.

b.  $|8| = 8$  because 8 is 8 units from 0.

c.  $|0| = 0$  because 0 is 0 units from 0.

40. a.  $|4| = 4$  because 4 is 4 units from 0.

b.  $|-7| = 7$  because  $-7$  is 7 units from 0.

41.  $-2 + 25 = 23$

42.  $8 + (-3) = 5$

43.  $2a - b = 2(8) - (-6) = 16 - (-6) = 16 + 6 = 22$

44.  $x - y = -2 - (-7) = -2 + 7 = 5$

45.  $-7 \cdot 3 = -21$

46.  $5(-2) = -10$

47.  $0 \cdot (-4) = 0$

48.  $-6 \cdot 9 = -54$

49.  $3(4-7) + (-2) - 5 = 3(-3) + (-2) - 5 = -9 + (-2) - 5 = -11 - 5 = -16$

50.  $4 - 8(7-3) - (-1) = 4 - 8(4) - (-1) = 4 - 32 - (-1) = 4 - 32 + 1 = -28 + 1 = -27$