## **Instructor's Manual for:**

Introductory Statistics for the Behavioral Sciences, 7th Ed. by J. Welkowitz, B. H. Cohen, and R. B. Lea

## **Answers to All Exercises**

## **Chapter 1**

1. (a) 
$$åX = 195$$
  $åX^2 = 2801$   $(åX)^2 = 38,025$ 

(b) 
$$å X = 138$$
  $å X^2 = 1512$   $(å X)^2 = 19,044$ 

(c) 
$$åX = 70$$
  $åX^2 = 550$   $(åX)^2 = 4,900$ 

(d) 
$$å X = 55$$
  $å X^2 = 685$   $(å X)^2 = 3,025$ 

2. (a) 
$$\sum X + \sum Y \text{ or } \sum (X + Y)$$

(b) 
$$\sum G + \sum P^2 \text{ or } \sum (G + P^2)$$

(c) 
$$\sum X^2 - 6\sum XY + 4(\sum X)^2 + 2\sum Y^2$$

3. (a) 
$$åX = 10$$
  $(åX)^2 = 100$   $å(X + Y) = 40$ 

$$åY = 30$$
  $(åY)^2 = 900$   $åX - åY = -20$ 

$$åX^2 = 30$$
  $å(X - Y) = -20$   $åXY = 73$ 

$$åY^2 = 206$$
  $åX + åY = 40$   $åXåY = 300$ 

(b) Rule 1: 
$$40 = 10 + 30$$

Rule 
$$2: -20 = 10 - 30$$

(c) 
$$å(X+k) = 10 + 20 = 30$$
;  $å(X+k) = 10 + 4 = 14$ ; Sum of new scores = 30

(d) 
$$å(Y-k) = 30-15=15; åY-k=30-3=27;$$
 Sum of new scores = 15

(e) 
$$å(kX) = 2*10 = 20$$
; Sum of new scores = 20

4. **Data set 1:** N = 5

$$\mathring{a}X = 7; \mathring{a}X^2 = 15; (\mathring{a}X)^2 = 49; \mathring{a}XY = 23; \mathring{a}(X+Y) = 18;$$
  $\mathring{a}Y = 11; \mathring{a}Y^2 = 39; (\mathring{a}Y)^2 = 121; \mathring{a}X\mathring{a}Y = 77; \mathring{a}(X-Y) = -4;$   $\mathring{a}(X^*3.2) = 7^*3.2 = 22.4; \mathring{a}(Y-7) = 11 - 5(7) = -24;$   $\mathring{a}(X+1.8) = 7 + 5(1.8) = 16; \mathring{a}(Y/4) = 11/4 = 2.75$ 

**Data set 2:** N=8

$$\mathring{a}X = 36.39; \mathring{a}X^2 = 253.04; \left(\mathring{a}X\right)^2 = 1324.23; \mathring{a}XY = 86.2; \mathring{a}\left(X+Y\right) = 56.46; \\ \mathring{a}Y = 20.07; \mathring{a}Y^2 = 76.74; \left(\mathring{a}Y\right)^2 = 402.80; \mathring{a}X\mathring{a}Y = 730.35; \mathring{a}\left(X-Y\right) = 16.32; \\ \Sigma(X*3.2) = 36.39*3.2 = 116.45; \Sigma(Y-7) = 20.07 - 8(7) = -35.93; \\ \Sigma(X+1.8) = 36.39 + 8(1.8) = 50.79; \Sigma(Y/4) = 20.07/4 = 5.02$$

5. **Data set 3:** N = 14

$$\Sigma X = 1,176; \Sigma X^2 = 100,288; (\Sigma X)^2 = 1,382,976; \Sigma XY = 96,426; å(X + Y) = 2,305$$
  
 $\Sigma Y = 1,129; \Sigma Y^2 = 93,343; (\Sigma Y)^2 = 1,274,641; \Sigma X \Sigma Y = 1,327,704; å(X - Y) = 47$ 

|       | Τι | Turck Kirk |   | irk | Dupre |    |
|-------|----|------------|---|-----|-------|----|
| Score | f  | cf         | f | cf  | f     | cf |
| 20    | 1  | 15         | 0 | 15  |       |    |
| 19    | 0  | 14         | 0 | 15  |       |    |
| 18    | 1  | 14         | 0 | 15  |       |    |
| 17    | 2  | 13         | 1 | 15  |       |    |
| 16    | 1  | 11         | 0 | 14  |       |    |
| 15    | 1  | 10         | 0 | 14  |       |    |
| 14    | 1  | 9          | 1 | 14  |       |    |
| 13    | 2  | 8          | 0 | 13  |       |    |
| 12    | 0  | 6          | 3 | 13  |       |    |
| 11    | 2  | 6          | 2 | 10  | 1     | 10 |
| 10    | 1  | 4          | 0 | 8   | 1     | 9  |
| 9     | 1  | 3          | 1 | 8   | 2     | 8  |
| 8     | 0  | 2          | 2 | 7   | 0     | 6  |
| 7     | 0  | 2          | 2 | 5   | 1     | 6  |
| 6     | 1  | 2          | 1 | 3   | 1     | 5  |
| 5     | 1  | 1          | 0 | 2   | 2     | 4  |
| 4     |    |            | 0 | 2   | 2     | 2  |
| 3     |    |            | 1 | 2   | 0     | 0  |
| 2     |    |            | 0 | 1   | 0     | 0  |
| 1     |    |            | 1 | 1   | 0     | 0  |

|       | Turck |    | Kirk |    |
|-------|-------|----|------|----|
| Score | f     | cf | f    | cf |
| 19–20 | 1     | 15 | 0    | 15 |
| 17–18 | 3     | 14 | 1    | 15 |
| 15–16 | 2     | 11 | 0    | 14 |
| 13–14 | 3     | 9  | 1    | 14 |
| 11-12 | 2     | 6  | 5    | 13 |
| 9–10  | 2     | 4  | 1    | 8  |
| 7–8   | 0     | 2  | 4    | 7  |
| 5–6   | 2     | 2  | 1    | 3  |
| 3–4   | 0     | 0  | 1    | 2  |
| 1–2   | 0     | 0  | 1    | 1  |
|       |       |    |      |    |

- 3. The Histogram is approximately symmetrical, and bimodal in shape.
- 4. The Turck polygon skews to the left, the Kirk polygon skews to the right, and both appear bimodal.

5.

| Stems<br>(Intervals) | Leaves<br>(Observations) |
|----------------------|--------------------------|
| 3 – 5                | 5                        |
| 6 - 8                | 6                        |
| 9 - 11               | 9011                     |
| 12 - 14              | 3 3 4                    |
| 15 – 17              | 5 6 7 7                  |
| 18 - 20              | 8 0                      |

- (2): a (5): d
- (3): a (6): g
- 7. (a) The *cf* corresponding to a score of 8 is 2;  $PR = (2/15) \times 100 = 13.33\%$ , so the PR for 8 is about 13.
  - (b) The cf for a score of 12 is 6;  $PR = (6/15) \times 100 = 40\%$ , so the PR for 12 is 40.
- 8. (a) A score of 16 corresponds to a *cf* of 14;  $PR = 14/15 \times 100 = 93.33$ .
  - (b) A score of 7 corresponds to a *cf* of about 4; PR ~  $4/15 \times 100 \sim 27$ .
- 9. (a) The desired  $cf = (25/100) \times 15 = 3.75$ , so the score at the 25th percentile is about 10.
  - (b) The desired  $cf = (75/100) \times 15 = 11.25$ , so the score at the 75th percentile is about 16.
- 10. (a) The 2nd decile at Kirk Hall corresponds to a cf of  $.2 \times 15 = 3$ , which corresponds to a score of 6.5 (i.e., the upper real limit of the 5–6 interval).
  - (b) The 50th percentile corresponds to a cf of  $.5 \times 15 = 7.5$ , which corresponds to a score of 9.5 (i.e., midway through the 9–10 interval).
  - (c) The 68th percentile corresponds to a cf of  $.68 \times 15 = 10$ , which corresponds to a score of about 11.