## Chapter 1—Introduction to corporate finance: Solutions to questions and problems

1 Presumably the current share value reflects the risk, timing and magnitude of all future cash flows, both short term and long term. If this is correct, then the statement is false.

2 Such organisations frequently pursue social or political missions, so many different goals are conceivable. One goal that is often cited is cost minimisation; that is, provide whatever goods and services at the lowest possible cost to society. A better approach might be to observe that even a not-for-profit business has equity. The equity is the desire to care for disadvantaged cases. Thus, one answer is that the appropriate goal is to maximise the value of the equity; that is maximise the care of needy cases.

3 The goal will be the same, but the best course of action toward that goal may be different because of differing social, political and economic institutions.

4 An argument can be made either way. At the one extreme we could argue that in a market economy all of these things are priced. There is therefore an optimal level of, for example, ethical and/or illegal behaviour, and the framework of share valuation explicitly includes these. At the other extreme we could argue that these are non-economic phenomena and are best handled through the political process. A classic (and highly relevant) question that illustrates this debate goes something like this: 'A firm has estimated that the cost of improving the safety of one of its products is $\$ 30$ million. However, the firm believes that improving the safety of the product will only save $\$ 20$ million in product liability claims. What should the firm do?'

Figure 1.9 clearly illustrates how a firm with multiple owners will face a dilemma. Different owners will have different preferences for Pl and P2 consumption. Owner C prefers more consumption now and less in P2. Owner A desires little consumption today, but more in P2. The three owners drawn in Figure 1.9 all want the firm to make different investment decisions. Owners A, B and C want the firm to invest at points $R, Q$ and $P$ respectively. Which owner does the firm please?

Fortunately, the firm does not have to make this difficult decision if a perfect capital market exists. As Figure 1.11 shows, the firm can make its investment decision independently of the owners' consumption preferences. It merely maximises the value of the firm by investing in all projects whose rate of return is greater than the market rate $(r>i)$. This is all opportunities up to point $Q$.

The firm sets its investment/dividend policy as follows:
P1 Invest $a_{1}: d_{1} \quad$ Pay $O: d_{1}$ as a period 1 dividend
P2 Projects return $O: d_{2}$ which is paid as dividend in period 2
If the owners don't like this dividend payout stream, they can use the capital
market to satisfy their preferences.
In Figure 1.11, Owner B prefers less P1 consumption and more P2 consumption than the firm is offering. In Pl , the owner gets a dividend of $O: d_{1}$ but the owner only wanted $O: f_{1}$. In P 2 , the owner gets a dividend of $O: d_{2}$ but the owner wanted $O: f_{2}$.

What the owner will do is invest the excess P1 dividend $\left(f_{1}: d_{1}\right)$ in the market, and spend the proceeds in P2. This enables the owner to move from point $Q$ up to point $B$. At point $B$ the owner's preferences are satisfied and the owner is actually on a higher utility curve than back in Figure 1.9 when a PCM did not exist.

Likewise, Figure 1.12 shows that all the firm needs to do is invest at point $Q$ and let the owners use the capital market to arrange their affairs so that consumption preferences are satisfied. This is Fisher's Separation Theorem: firms can separate their investment decisions from the owners' preferences. The existence of a PCM is crucial to this theorem.

## 6 Firm decisions with imperfect capital markets

Consider Figure 1.14 where $i_{1}<i<i_{b}$ (i.e. the lending or investing interest rate is less than the borrowing interest rate).

Imperfections in the capital market have led to a situation in which the borrowing and lending rates may differ. For borrowers the optimal point of production is $Y_{b}$, and for lenders the optimal point is $Y_{L}$. Thus, when borrowing and lending rates differ (i.e. there are imperfections in the market), there is no longer a unique production decision that would be made by any current owner regardless of the owner's tastes: Arrow's Impossibility Theorem.

Note that market imperfections cannot exist in a competitive market.

7 A firm with many owners should invest in all projects whose rate of return exceeds what the firm could get from investing the money in the capital market (i.e. $r>i$ ).

It is a simple calculation to derive the rate of return which will be earned on each proposal. Proposal 1 gives a return of $(240000-200000) \div \div 200000=20 \%$. This means Proposal 1 is desirable because, if we did not invest in it, the best we could do is to invest the $\$ 200000$ in the market, which would only provide a return of $\$ 220000(\$ 200000 \times 1.10)$. On the other hand, Proposal 2 gives a return of $(210000-200000) \div 200000=5 \%$. The firm should not invest in this proposal because it can earn a higher return ( $10 \%$ ) from the market.
Proposal $\quad$ Outlay (\$) return (\$) \% return

| 1 | 200000 | 240000 | 20.0 |
| ---: | ---: | ---: | ---: |
| 2 | 200000 | 210000 | 5.0 |
| 3 | 200000 | 215000 | 7.5 |
| 4 | 200000 | 218000 | 9.0 |
| 5 | 200000 | 225000 | 12.5 |
| 6 | 200000 | 220000 | 10.0 |

Therefore, the firm will only invest in Proposals 1 and 5. It would be indifferent to proposal 6.
b Proposals 1 and 5 will require an investment of $\$ 400000$ (today - period 1). Of the initial endowment of $\$ 1000000$, this leaves $\$ 600000$ excess, which will be paid as the period 1 dividend. Proposals 1 and 5 return $\$ 240000$ and $\$ 225000$ respectively, which means the period 2 dividend will be $\$ 465000$.
c The share capital of the firm consists of 10000 shares. Therefore, the dividend per share will be $\$ 60$ in period $1(600000 \div 10000)$ and $\$ 46.50$ in period $2(465000$ $\div 10000$ ).

By following the investment and dividend strategy outlined above, the value of the firm will be maximised. All shareholders will receive per share dividends of $\$ 60$ in Pl and $\$ 46.50$ in P2, regardless of their preferences between P1 and P2 consumption. As we shall see below, the existence of a capital market enables shareholders to achieve their desired P1 and P2 consumptions. That is, if the $\$ 60-$ $\$ 46.50$ payout does not suit the shareholder, the shareholder can invest or borrow in the market to exactly achieve their desired outcomes. This will demonstrate Fisher's Separation Theorem: firms do not need to worry about the consumption preferences of each individual owner; their job is simply to maximise the value of the firm.
d An owner of 2000 shares will receive a dividend stream of:
Period $1 \quad \$ 60 \times 2000 \quad=\$ 120000$
Period $2 \quad \$ 46.50 \times 2000=\$ 93000$

The question is really saying that this stream does not suit the shareholder. The shareholder has a stronger preference for consumption next year and only wishes to consume $\$ 10000$ today. The shareholder will invest the excess $\$ 110000$ (120 000-10000) in the capital market at $10 \%$ interest.

This investment will mature next year and will be worth $\$ 121000(110000 \times$ 1.10). Combined with the P2 dividend of $\$ 93000$, the shareholder can consume $\$ 214000(121000+93000)$ in P2.

The shareholder in this part has a stronger preference for consumption today and is less concerned about next year's consumption. Although they will receive $\$ 93000$ in dividends next year, this is more than they desire ( $\$ 50000$ ). The shareholder will use the capital market to borrow against the excess future dividend ( $93000-50000$ ) and consume that money today. This means they will
move down the market line.
Next year's $\$ 93000$ dividend will be used as follows:

- $\quad \$ 50000$ required for consumption
- $\quad \$ 43000$ excess dividend used to pay off borrowing.

Therefore, the shareholder will borrow an amount of money in Pl which will be precisely paid off by the excess $\$ 43000$ in P2. That is, in P1 borrow $\$ 39090.91$ (43 $000 \div 1.10$ ). This enables consumption today of $\$ 159090.91$ (120 $000+$ 39090.91 ).

This question has illustrated how the firm does NOT need to worry (or even be aware) of the owners' consumption preferences. As long as the capital market exists, the owners can arrange their affairs to meet their consumption preferences.

8a Refer to Figure 1.15. $Q$ is the optimal point of production for the firm. At this point, the wealth and utility of all owners is maximised (puts them on highest utility curve). To reach point $Q$, the firm must invest $a_{1} d_{1}$ in available projects.

In practice, how does the firm know what $a_{1} d_{1}$ is? It employs one of the following two investment rules.

## NPV rule

In a two-period world, the NPV rule is as follows:
$\mathrm{NPV}=\frac{\mathrm{X}_{2}}{1+\mathrm{i}}-\mathrm{I}_{1}$
The NPV compares the initial outlay required by the project (I) against the return in P2 from the project $\left(X_{2}\right)$ in present value terms. The decision rule is:

| if NPV | +ve | accept project |
| :--- | :--- | :--- |
| if NPV | - ve | reject project |
| if NPV | 0 | indifferent |

It follows that the value of the firm will change according to the NPV of projects undertaken. If we invest in positive NPV projects, the firm value increases by the NPV, and if we invest in negative NPV projects the firm value will fall by the NPV.

## IRR rule

The second decision rule is IRR, which is found by solving for $r$ in the following equation:
$\frac{X_{2}}{1+r}=I_{1}=0$

The IRR figure $(r)$ is an average rate of return from the project over its duration. This figure must be compared to the opportunity cost of funds (the return which the firm could have earned in the market).

The accept/reject decision rule for IRR is:
if $r>i \quad$ accept
if $r<i \quad$ reject
if $r=i \quad$ indifferent
Given that $r$ and $i$ represent the slopes of the production frontier and market line in Figure 1.14 respectively, we can see that the IRR rule is merely accepting all projects up to the point where the next project provides the same return as that available in the market (i.e. point $Q$ ).

The NPV and IRR rules are essentially the same, in that they give the same accept/reject decisions for projects.
b The issue of optimal capital structure (D/E) relates to the financing decision of the firm. That is, do we use equity or debt funding?

Under conditions of certainty and perfect capital markets, there is only one interest rate prevailing in the market, and this is the riskless rate $i$. Because there is no risk, there is no real distinction between the equity securities which a firm might issue and its debt securities. Consequently, questions of capital structure (combinations of debt and equity) do not exist. The only relevant question is the amount of funds required by the firm.
c The dividend decision (how much dividend we pay) does not affect firm value. Figure 1.17 shows that the firm can borrow money to pay any amount of dividends in period 1 as they wish. In Figure 1.17, the firm has already borrowed $O b_{1}$ to finance all profitable projects (up to point $Q$ ), and can borrow even more money $\left(b_{1} b_{2}\right)$ to pay a Pl dividend.

Of course, all money borrowed in P1 must be repaid in P2 with interest. This means that the P2 dividend will be less than it would have been had a P1 dividend not been paid. But the PV of both dividends $(\mathrm{P} 1+\mathrm{P} 2)$ will be the same. Hence, by borrowing money to pay a P1 dividend, the firm is only trading P2 dividends for P1 dividends, without any effect on total owner wealth.

9a There is a $\$ 1 \mathrm{~m}$ spending constraint. It is not good enough to rank the individual projects in order of return and then accept them in order. You need to look at all the possible combinations of projects whose combined outlay is less than or equal to $\$ 1 \mathrm{~m}$, and select the combination with the highest NPV.

However, a quick calculation of NPVs may reveal a project not even worth considering:

| Project | Outlay (\$) | Present value of <br> expected cash | NPV |
| :--- | :--- | :--- | :--- |

Solutions manual t/a Fundamentals of Corporate Finance 7e, Ross et al

|  |  | flow (\$) |  |
| :---: | :---: | :---: | :---: |
| 1 | 500000 | 610000 | 110000 |
| 2 | 150000 | 142500 | -7500 |
| 3 | 350000 | 420000 | 70000 |
| 4 | 450000 | 531000 | 81000 |
| 5 | 200000 | 240000 | 40000 |
| 6 | 400000 | 420000 | 20000 |

This reveals that Project 2 has a negative NPV and should not be considered. Note that the returns from each project are already expressed in PV terms. Therefore, there is no need to discount those cash flows at $10 \%$. Students: be careful to note whether the cash flows given to you are in PV terms or not.

Also, this question is not necessarily within a two-period world. We do not know the duration of the suggested projects or the pattern of returns. We only know their PV. For example, the $\$ 610000$ PV of cash flows from Project 1 may represent cash inflows over a 10 -year period discounted at $10 \%$.

Below is a schedule of all combinations of projects having an investment outlay of $\$ 1 \mathrm{~m}$ or less.

| Combo | Projects | PV of outlay <br> $(\$)$ | Total cash <br> flow (\$) | NPV (\$) |
| :---: | :---: | :---: | ---: | ---: |
| A | 1,3 | 850000 | 1030000 | 180000 |
| B | 1,4 | 950000 | 1141000 | 191000 |
| C | 1,5 | 700000 | 850000 | 150000 |
| D | 1,6 | 900000 | 1030000 | 130000 |
| E | 3,4 | 800000 | 951000 | 151000 |
| F | 3,5 | 550000 | 660000 | 110000 |
| G | 3,6 | 750000 | 840000 | 90000 |
| H | 4,5 | 650000 | 771000 | 121000 |
| I | 4,6 | 850000 | 951000 | 101000 |
| J | 5,6 | 600000 | 660000 | 60000 |
| K | $3,4,5$ | 1000000 | 1191000 | 191000 |
| L | $3,5,6$ | 950000 | 1080000 | 130000 |

The firm is indifferent between Proposals B and K. Any unused funds (\$50 000 for Proposal B) can be retained by the firm and invested at market rate $=10 \%$, or paid out immediately as a dividend.
Proposal K Spend \$1000 000 and give a PV of cash flow of \$1 191000 = NPV of \$191 000

Proposal B Spend \$950 000 and give a PV of cash flow of \$1 141000 = NPV of \$191 000

The surplus $\$ 50000$ can be invested or paid as a dividend. If invested at $10 \%$, this gives $\$ 55000$ return in year 2 . PV of $\$ 55000=(55000 \div 1.10)=\$ 50000$.

NPV of this $=50000-50000=$ ZERO

[^0]NPV = \$191 000 + zero = \$191 000
b The current soft capital rationing policy (not investing more than $\$ 1 \mathrm{~m}$ ) is not maximising the value of the firm. As calculated above, it is $\$ 191000+$ initial endowment under the policy.

However, all projects (with the exception of Project 2) have a positive NPV. If there were no spending restraints we would invest in Projects $1,3,4,5$ and 6. This would require $\$ 1900000$ in outlays but would bring in $\$ 2221000$ in PV of cash flows.

This represents a total NPV of $\$ 321000$, compared to a NPV of $\$ 191000$ provided by proposal B or K. Hence, the value of the firm is $\$ 130000(321000-$ 191 000) less than its optimal value due to the spending constraint.

10a $\quad \$ 500000$ is the maximum limit on spending. We need to look at all combinations of projects whose total investment required is less than or equal to $\$ 500000$ and choose the one that provides the largest total dollar return.

|  | Outlay (\$) | Period 1 <br> dividend | Period 2 <br> dividend | Firm <br> value | NPV (\$) |
| :--- | ---: | :---: | :---: | ---: | :---: |
| 1 | 450000 | 50000 | 565000 | 532906 | 32906 |
| 1 | 300000 | 200000 | 415000 | 554700 | 54700 |
| 1 | 350000 | 150000 | 432500 | 519658 | 19658 |
| 1 | 500000 | nil | 585000 | 500000 | nil |
| 3 | 450000 | 50000 | 557500 | 526496 | 26496 |

(i) Projects 1 and 3 .
(ii) Total investment $\$ 300000$.
(iii) This will leave a $\$ 200000$ period 1 dividend.
(iv) The period 2 dividend will be $\$ 415000$.
(v) Firm value $=$ present value of period 1 and period 2 dividend payments $\quad=\quad \$ 200000+\$ 415000 \div(1+17 \%)$

$$
=\$ 554700
$$

$\mathrm{b} \quad$ The temptation is to pick the project with the highest rate of return: Project 1 with $45 \%$. However, remember that positive NPV projects increase firm value. The firm's aim is not to maximise rate of return (IRR is a percentage type of
figure). The aim is to maximise NPV. Therefore, Project 3, if selected by itself, will maximise the present value of dividends. The period 1 dividend is the surplus $\$ 300000$ and the period 2 dividend is the $\$ 270000$ return from Project 3.

|  | Outlay (\$) | $\boldsymbol{P}_{2}$ return (\$) | PV of $\boldsymbol{P}_{2}$ <br> return (\$) | NPV (\$) | Dividend <br> surplus $(\$)$ | Firm <br> value $(\$)$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 100000 | 145000 | 123932 | 23932 | 400000 | 523932 |
| 2 | 350000 | 420000 | 358974 | 8974 | 150000 | 508974 |
| 3 | 200000 | 270000 | 230769 | 30769 | 300000 | 530769 |
| 4 | 250000 | 287500 | 245727 | $(4273)$ | 250000 | 495727 |
| 5 | 400000 | 440000 | 376068 | $(23932)$ | 100000 | 476068 |


|  | Outlay (\$) | P2 return <br> (\$) | PV of $\mathbf{P}_{\mathbf{2}}$ <br> return (\$) | NPV (\$) | IRR (\%) |
| :---: | ---: | ---: | ---: | ---: | ---: |
| Project | IR |  |  |  |  |
| 1 | 100000 | 145000 | 123932 | 23932 | 45 |
| 2 | 350000 | 420000 | 358974 | 8974 | 20 |
| 3 | 200000 | 270000 | 230769 | 30769 | 35 |
| 4 | 250000 | 287500 | 245727 | $(4273)$ | 15 |
| 5 | 400000 | 440000 | 376068 | $(23932)$ | 10 |

Hence, the firm would accept Projects 1, 2 and 3, and reject Projects 4 and 5.
(ii) The funds required are $\$ 650000$.
(iii) Given the initial endowment of $\$ 500000$, they will need to borrow $\$ 150000$ if they are to reach their optimal investment level.
(iv) If they borrow exactly $\$ 150000$, then there are no funds for a period 1 dividend. The period 2 dividend will be the return from Projects 1,2 and 3: $\$ 835000$ less the repayment of the funds borrowed and interest ( $150000 \times 117 \%=175500$ ) gives $\$ 659500$.
(v) Firm value $=$ present value of period 1 and period 2 dividend payments

$$
\begin{aligned}
& =\text { nil }+\$ 659500 /(1+17 \%) \\
& =\$ 563675 \\
& =\text { initial endowment }(\$ 500000)+\text { NPV of Projects } 1,2 \\
& \text { and } 3(\$ 63675)
\end{aligned}
$$

(vi) Yes, the value of the firm has increased by $\$ 8975$ (563 675-554 700) when the capital rationing policy was removed. This indicates that capital rationing of any description may lead to a suboptimal firm value.
d (i) If the firm wanted to pay a period 1 dividend of $\$ 100000$, it would have to borrow an additional $\$ 100000$ (in addition to the first

[^1](ii) The period 2 dividend will be the same as before, less the second lot of borrowing + interest $(100000 \times 117 \%=\$ 117000)$. Hence, $\$ 542500$.
(iii) Firm value $=$ present value of period 1 and period 2 dividend payments
\[

$$
\begin{aligned}
& =\$ 100000+\$ 542500 /(1+17 \%) \\
& =\$ 563675
\end{aligned}
$$
\]

This is the same firm value as in part $\mathrm{c}(\mathrm{v})$ above. The fact that the firm borrowed $\$ 100000$ to pay a period 1 dividend has not changed the value. It merely represents a trade-off made by the shareholders of period 2 consumption for period 1 consumption. Hence, dividend policy (and financing policy) is irrelevant to firm value.

11a

| Project | Period 2 <br> cash (\$) | Outlay (\$) | IRR (\%) | NPV (\$) |
| :---: | ---: | ---: | ---: | ---: |
| 1 | 152250 | 121800 | 25.0 | 16609 |
| 2 | 125425 | 98760 | 27.0 | 15263 |
| 3 | 118250 | 110000 | 7.5 | -2500 |
| 4 | 121555 | 105700 | 15.0 | 4805 |

b Accept Project 1, the highest NPV.
c $\quad$ Acceptable investments are 1, 2 and 4. Outlay $=\$ 121800+\$ 98760+\$ 105700$ = \$326 260
Borrow \$26 260 at 10\% and repay \$28 886
Period 1 dividend $=$ nil
Period 2 dividend $=152250+125425+121555-28886=\$ 370344$
$\mathrm{NPV}=\$ 370344 \div 1.1-\$ 300000=\$ 36677$
IRR \$16 $609+\$ 15263+\$ 4805=\$ 36677$

| Project | Outlay (\$) | IRR (\%) | P2 (\$) | NPV (\$) |
| :---: | ---: | ---: | ---: | ---: |
| 1 | 110000 | 22 | 134200 | 12000 |
| 2 | 60000 | 30 | 78000 | 10909 |


| 3 | 76000 | 9 | 82840 | -691 |
| ---: | ---: | ---: | ---: | ---: |
| 4 | 90000 | 17 | 105300 | 5727 |
| 5 | 93000 | 6 | 98580 | -3382 |


| Funds available | $\$ 500000$ |
| :--- | :--- |
| Total outlays | $\$ 260000$ |
| Available for Dividend 1 (D1) | $\$ 240000$ |
| J Low's share (10\% of D1) | $\$ 24000$ |

Available for Dividend 2 (D2)
$=\$ 110000(1.22)+\$ 60000(1.3)+\$ 90000(1.17)$
$=\$ 134200+\$ 78000+\$ 105300=\$ 317500$
J Low's share ( $10 \%$ of D2) $=\$ 31750$
c
Accept Projects 1, 2 and 4 because the IRR is greater than $10 \%$.
$\mathrm{NPV}=\$ 12000+\$ 10909+\$ 5727=\$ 28636$
Value of the firm $=\$ 500000+\$ 28636=\$ 528636$
b

| In period 1 J Low receives | $=\$ 23000$ |
| :--- | :--- |
| She borrows | $=\$ 50000-\$ 23000$ |
| She repays | $=\$ 27000(1.1)$ |
| Period 2 expenditure | $=\$ 32850-\$ 29700$ |
|  | $=\$ 29700$ |
|  |  |

13

## Figure 1.15

The firm's investment decision


| Project | P2 (\$) | Outlay (\$) | IRR (\%) | NPV (\$) |
| :---: | ---: | ---: | ---: | ---: |
| 1 | 122000 | 100000 | 22.0 | 10909 |
| 2 | 65000 | 50000 | 30.0 | 9091 |
| 3 | 93740 | 86000 | 9.0 | -782 |
| 4 | 107640 | 92000 | 17.0 | 5855 |
| 5 | 100700 | 95000 | 6.0 | -3455 |


| Initial endowment | $o a$ | $\$ 200000$ |
| :--- | :--- | :--- |
| Borrowings | $o b_{1}$ | $\$ 42000$ |
| Repayment | $P B \$ 42000(1.1)$ | $\$ 46200$ |
| NPV | $a A$ | $\$ 25855$ |
| Value $=\$ 200000+\$ 25855=O A$ | $\$ 225855$ |  |

or
$(\$ 122000+\$ 65000+\$ 107640-\$ 46200) / 1.1 \quad \$ 225855$

14a $\quad \mathrm{NPV}=\$ 5470 \div 1.08-\$ 5000=(\$ 64.81)$
b $\quad \mathrm{IRR}=\$ 7590 / \$ 6600-1=15 \%$
c

| Project | P2 | Outlay (\$) | IRR (\%) | NPV ( $\$$ ) |  |
| :---: | :---: | ---: | ---: | ---: | :---: |
| A | 2460 | 2000 | 23.0 | 278 | Accept |
| B | 5900 | 5000 | 18.0 | 463 | Accept |
| C | 7460 | 7000 | 6.6 | -93 | Reject |
| D | 3340 | 3000 | 11.3 | 93 | Accept |
| E | 10800 | 10000 | 8.0 | 0 | Indifferent |
| F | 6680 | 6000 | 11.3 | 185 | Accept |

Invest in $\mathrm{A}, \mathrm{B}, \mathrm{D}$ and F .
d Total available period $2=\$ 2460+\$ 5900+\$ 3340+\$ 6680=\$ 18380$
Funds invested (A, B, D and F) $=\$ 16000$
Funds remaining after investment $=\$ 20000-\$ 16000 \quad=\$ 4000$
Amount to be borrowed $=\$ 10000-\$ 4000 \quad=\$ 6000$
Repayment $=\$ 6000 \times 1.08 \quad=\$ 6480$
Balance available period $2=\$ 18380-\$ 6480 \quad=\$ 11900$
e Acceptable projects are A, B, D and E.
Combined outlays $=\$ 16000$
Available savings $=\$ 13000$
Funds to borrow $=\$ 3000$
f Available funds period $2=\$ 18380$
Repayment $=\$ 3000 \times 1.08=\$ 3240$
Balance period $2=\$ 15140$
Period 1 dollars $=\$ 15$ 140/1.08 $=\$ 14019$
Increase in wealth $=\$ 14019-\$ 13000=\$ 1019$
g Without borrowing there is $\$ 13000$ to invest, so accept Projects A, B and F.
$\begin{array}{ll}\text { Outlay }=\$ 2000+\$ 5000+\$ 6000 & =\$ 13000 \\ \text { Period } 2 \text { cash flow }=\$ 2460+\$ 5900+\$ 6680 & =\$ 15040 \\ \text { In period } 1 \text { dollars }=\$ 15040 / 1.08 & =\$ 13926 \\ \text { Increase in wealth }=\$ 13926-\$ 13000 & =\$ 926\end{array}$
By borrowing, the increase in wealth changes from $\$ 926$ to $\$ 1019$. You are $\$ 93$ better off by borrowing. The $\$ 93$ is the NPV of investment D. Accept investments as long as you can identify returns higher than the market rate of return or equivalently accept investments where the present value is greater than the outlay when the present value is derived using the market rate of return even if you have to borrow.

15 a to c
Helen can borrow against her future income as follows:
Helen will receive $\$ 99000$ in period 1.
Requires $\$ 60000+\$ 50000=\$ 110000$
Shortage in period $1=\$ 110000-\$ 99000=\$ 11000$ (c)
Helen will borrow \$11 000.
She will need to repay in period $2 \$ 11000 \times 1.08=\$ 11880$
Helen will receive $\$ 115825$ in period 2
Requires $\$ 65000+\$ 11880 \quad=\$ 76880$
Surplus in period $2=\$ 115825-\$ 76880=\$ 38945$ (b)

16 The projects have been ranked in terms of IRR.

| Project | Outlay (\$) | P2 (\$) | Profit (\$) | NPV (\$) | IRR (\%) |
| :---: | ---: | ---: | ---: | ---: | ---: |
| G | 615000 | 744150 | 129150 | 61500 | 21 |
| E | 490000 | 588000 | 98000 | 44545 | 20 |
| F | 530050 | 630760 | 100710 | 43368 | 19 |
| D | 875000 | 1023750 | 148750 | 55682 | 17 |
| A | 305555 | 351388 | 45833 | 13889 | 15 |
| C | 1792600 | 2043564 | 250964 | 65185 | 14 |
| B | 472890 | 524908 | 52018 | 4299 | 11 |

The project with the greatest IRR is Project G. This project produces the combination of $\$ 4466095$ in P1 and $\$ 744150$ in P2. The projects were ranked on the basis of IRR as the slope of the production possibility frontier is the IRR.

|  | $\boldsymbol{P 1}(\$)$ | $\boldsymbol{P 2}(\$)$ |
| :---: | ---: | ---: |
|  | 5081095 | 0 |
| Accept G | 4466095 | 744150 |
| Plus E | 3976095 | 1332150 |
| Plus F | 3446045 | 1962910 |
| Plus D | 2571045 | 2986660 |
| Plus A | 2265490 | 3338048 |
| Plus C | 472890 | 5381612 |
| Plus B | 0 | 5906520 |

When the market rate of interest is $10 \%$, all projects are acceptable. The market rate of interest must be greater than $11 \%$ before you would start to reject projects on the basis of negative NPVs or where $r$ is less than $i$.


If the project developer undertakes all projects with a positive NPV, the wealth of the developer will increase.

17 If the developer were to set a cut off for project acceptability at $15 \%$ (being one and a half times the market rate of interest), the developer would reject Projects C and B, which have a combined NPV of $\$ 69$ 485. The developer is not maximising the value of the firm by foregoing projects worth an extra $\$ 69485$ in firm value.

The question of risk is addressed in later chapters. At this stage, NPV is calculated as the future cash flows discounted at some rate that reflects risk. If the uncertainty or risk is correctly reflected in the interest rate used to convert future periods to current periods, then the NPV reflects the increase in value or wealth after accounting for the risk.

The increase in risk will probably increase the rate used to calculate the NPV.

18 Current value of Film Promotions
Cash not invested
Therefore current value of $\mathrm{P}_{2}$ cash flow
$\mathrm{P}_{2}$ cash flow in $\mathrm{P}_{2}$ dollars
$=12650000$
Return from investment $=12650000 \div 8000000-1=.58125$ or $58.125 \%$.

19 The rate of return for the firm is determined by its ability to transform period 1 dollars into future period dollars; that is, the opportunities provided by the investment proposals it can select. In the simple two-period model, it has been
shown as the production possibility frontier, where some of the firm's investment return is more than the market rate of return. When the firm only accepts projects with a return greater than or equal to the market rate of return, then its return must be greater than the market rate.

No, it is not possible given the assumptions. Perfect certainty means there is no difference between debt and equity in Gary's Logistics, therefore both securities would have to earn at least 16 per cent. If there is uncertainty, then the risk of equity will be greater than the risk of debt (there will be more discussion on this in later chapters). We will see that the higher the risk, the higher the return. The perfect capital market means all investors will have access to all information so they will all require the same return. As rational investors, they will want more return in order to increase their utility.

21 Perfect certainty simply means that the future is known with certainty. There is no need to estimate future cash flows and returns. A perfect capital market exists if a number of conditions hold: namely that all participants have access to all available information and all may participate in the market freely. There is no market interference or externalities such as monopolies or government restrictions or conditions where some investors or borrowers may get better conditions than others.

## MINICASE ANSWERS

1 The advantages of changing from a sole proprietorship to a company include:
(i) separation of ownership from management, allowing for sale/transfer of ownership and not limiting the lifespan of the company to the individual owner
(ii) a company is a legal entity and can borrow money and act in its own name, therefore shareholders have limited liability, unlike sole proprietors who have unlimited liability.

2 Changing to a company structure should help the McGees grow their business. The ability to borrow in a company name and/or obtain equity funding by selling a part of the company to others would allow them to invest the needed funds in assets (equipment) and employ more staff to deal with the increased demand for their product.

3 Recommend the McGees change to a company structure to get the benefit of borrowings and equity to grow the business. Company structure also gives them an option to scale back their hands-on involvement and/or sell out of the business when it reaches its most successful point.


[^0]:    Solutions manual t/a Fundamentals of Corporate Finance 7e, Ross et al Copyright © 2016 McGraw-Hill Education (Australia) Pty Ltd

[^1]:    Solutions manual t/a Fundamentals of Corporate Finance 7e, Ross et al Copyright © 2016 McGraw-Hill Education (Australia) Pty Ltd

