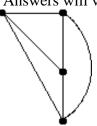
## Chapter 2: Business Efficiency

## Free-Response

Format: Short Answer

1. Construct a complete graph on four vertices.

Ans: Answers will vary. One solution is:

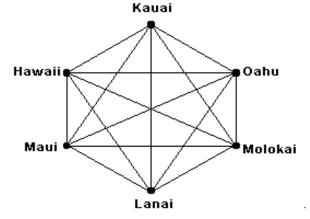


Format: Short Answer

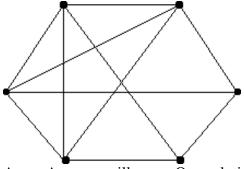
2. Construct a complete graph whose vertices represent the six largest islands of Hawaii:

Kauai, Oahu, Molokai, Lanai, Maui, and Hawaii.

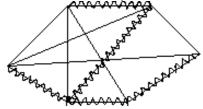
Ans: Answers will vary. One solution is:



3. Construct an example of a spanning tree on the graph given below.



Ans: Answers will vary. One solution is:



Format: Short Answer

4. Construct an example of a graph with no Hamiltonian circuit.

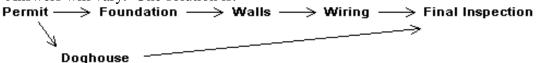
Ans: Answers will vary. One solution is:



Format: Short Answer

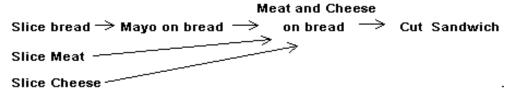
5. Construct a digraph for the following tasks necessary when building a house: get a building permit, install wiring, pour foundation, build walls, build doghouse, pass final inspection.

Ans: Answers will vary. One solution is:



6. Identify six tasks necessary when building a sandwich, and construct a digraph for these tasks.

Ans: Answers will vary. One solution is:



Format: Short Answer

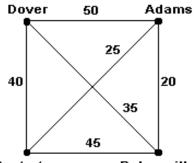
7. Identify six tasks necessary when preparing for a picnic, and construct a digraph for these tasks.

Ans: Answers will vary. One solution is:



Format: Short Answer

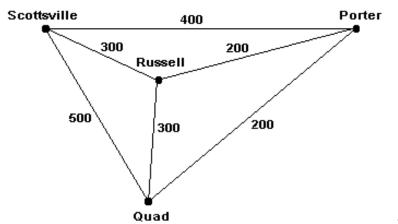
8. Use the brute force algorithm to solve the traveling salesman problem for the graph of the four cities shown below.



Centertown Bakersville

Ans: Route ABCDA and ACBDA have cost 155. Route ABDCA has (minimum) cost 120.

9. Use the brute force algorithm to solve the traveling salesman problem for the graph of the four cities shown below.



Ans: Route PQRSP and PQSRP have (minimum) cost 1200. Route PRQSP has cost 1400.

Format: Short Answer

10. If a graph of nine vertices is complete, how many edges are there?

Ans: (9)(8)/2=36 edges

Format: Short Answer

11. You own a chain of 12 apartment complexes (including your residence) and you want to plan a trip to visit each of your properties. If it takes 1/2 minute to compute the total length of a tour, how long will it take to apply the brute force algorithm to find the optimal tour?

Ans: (11!/2)(1/2) = 9,979,200 minutes, or approximately 19 years

Format: Short Answer

12. You own a chain of 10 one-day photo development kiosks and a lab where the photos are developed. Each morning and evening a delivery truck leaves the lab, visits each kiosk, and returns to the lab. If it takes 1/3 minute to compute the total length of a tour, how long will it take to apply the brute force algorithm to find the optimal tour for the delivery truck?

Ans: (9!/2)(1/3) = 60,480 minutes, or 42 days

Format: Short Answer

13. You want to create a mileage grid showing the distance between every pair of the 50 U.S. state capitals. How many numbers will you have to compute?

Ans: (50)(49)/2 = 1225

14. You want to create a mileage grid showing the distance between every pair of the 10 Canadian provincial and territorial capitals. How many numbers will you have to compute?

Ans: (10)(9)/2 = 45

Format: Short Answer

15. The local cafe offers three different entrees, 10 different vegetables, and four different salads. A "blue plate special" includes an entree, a vegetable, and a salad. How many different ways can a special be constructed?

Ans: 120

Format: Short Answer

16. A nearby ice cream shop offers 31 different flavors and three different types of cones. How many different single scoop cones can be ordered?

Ans: 93

Format: Short Answer

17. In some states, license plates use a mixture of letters and numerals. How many possible plates could be constructed using three letters followed by three numerals?

Ans:  $26^3 \times 10^3 = 17,576,000$ 

Format: Short Answer

18. In some states, license plates use a mixture of letters and numerals. How many possible plates could be constructed using three letters followed by four numerals?

Ans:  $26^3 \times 10^4 = 175,760,000$ 

Format: Short Answer

19. What is an advantage of a heuristic algorithm?

Ans: Fast

Format: Short Answer

20. What is a disadvantage of a *heuristic* algorithm?

Ans: Not always optimal

21. What is *critical* about the *critical path* of an order-requirement digraph?

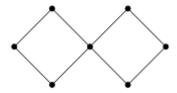
Ans: It requires the critical or essential amount of time required to complete the

project.

Format: Short Answer

22. Construct a graph which has an Euler circuit, but not a Hamiltonian circuit.

Ans: Answers may vary. One solution is:



Format: Short Answer

23. Can a graph have a Hamiltonian circuit, but not an Euler circuit?

Ans: Yes

Format: Short Answer

24. Will the nearest-neighbor algorithm ever use the most expensive edge of a graph?

Ans: Yes

Format: Short Answer

25. The route of a neighborhood garbage truck generally follows an Euler circuit. Under what circumstances should it instead follow a Hamiltonian circuit?

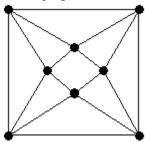
Ans: If it only picks up at the intersection of streets

Format: Short Answer

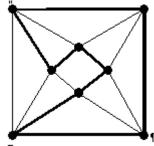
26. The route of a delivery truck generally follows a Hamiltonian circuit. Under what circumstances should it instead follow an Euler circuit?

Ans: If it delivers to houses on the sides of streets

27. In the graph below, construct a Hamiltonian circuit.

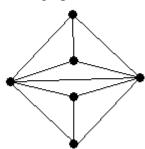


Ans: Answers will vary. One solution is:

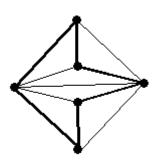


Format: Short Answer

28. In the graph below, construct a Hamiltonian circuit.

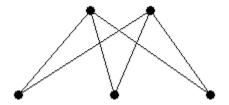


Ans: Answers will vary. One solution is:



29. Construct an example of a connected graph that does not have a Hamiltonian circuit.

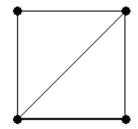
Ans: Answers will vary. One solution is:



Format: Short Answer

30. Construct an example of a connected graph that has a Hamiltonian circuit but does not have an Euler circuit.

Ans: Answers will vary. One solution is:



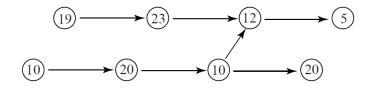
Format: Short Answer

31. A connected graph H has a spanning tree with 50 edges. How many vertices does the spanning tree have? How many vertices does H have? What can one say about the number of edges H has?

Ans: The spanning tree has 51 vertices. H also has 51 vertices. H must have at least 50 edges.

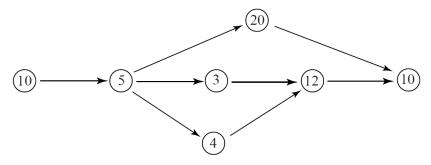
Format: Short Answer

32. Find the earliest completion time for the following order-requirement digraph.



Ans: 60

33. Find the earliest completion time for the following order-requirement digraph.

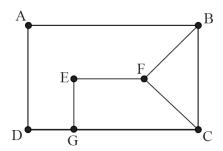


Ans: 45

Chapter 2 Free-Response

Format: Short Answer

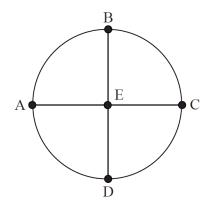
34. How many distinct Hamiltonian circuits can you find on the following graph?



Ans: One: ADGEFCBA

Format: Short Answer

35. How many distinct Hamiltonian circuits can you find on the following graph? (Do not count a circuit and the reverse of the same circuit as distinct.)



Ans: Four: ABECDA, ABCEDA, AEDCBA, AEBCDA

Format: Short Answer

36. If you add a new vertex to a complete graph of 10 vertices, how many new edges are needed to make the new graph complete?

Ans: 10