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111 | For a 180-lb person :

$$W = mg : 180 \text{ lb} = m (32.2 \text{ ft/sec}^2)$$

$$m = \underline{5.59 \text{ slugs}}$$

$$180 \text{ lb} \left( \frac{4.4482 \text{ N}}{\text{lb}} \right) = \underline{801 \text{ N}}$$

$$W = mg : 801 \text{ N} = m (9.81 \text{ m/s}^2)$$

$$m = \underline{81.6 \text{ kg}}$$

1/3 | The weight of an average apple is

$$W = \frac{5 \text{ lb}}{12 \text{ apples}} = 0.417 \text{ lb}$$

$$\text{Mass in slugs is } m = \frac{W}{g} = \frac{0.417}{32.2} = \underline{0.01294 \text{ slugs}}$$

$$\text{Mass in kg is } m = 0.01294 \text{ slugs} \left( \frac{14.594 \text{ kg}}{1 \text{ slug}} \right) \\ = \underline{0.1888 \text{ kg}}$$

$$\text{Weight in N is } W = mg = 0.1888 (9.81) = \underline{1.853 \text{ N}}$$

These apples weigh closer to 2 N each than to the rule of 1 N each!

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$r = 0.050$  m for both spheres

$$F = \frac{G m_c m_t}{d^2} = \frac{G \left( \rho_c \frac{4}{3} \pi r^3 \right) \left( \rho_t \frac{4}{3} \pi r^3 \right)}{d^2}$$
$$= \frac{G \rho_c \rho_t \left( \frac{4}{3} \pi r^3 \right)^2}{d^2}$$

$$\text{With } \begin{cases} G = 6.673 (10^{-11}) \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2} \\ \rho_c = 8910 \text{ kg/m}^3 \\ \rho_t = 3080 \text{ kg/m}^3, \end{cases}$$

We obtain, as vectors:

$$(a) \quad \underline{F} = - 1.255 (10^{-10}) \underline{i} \text{ N} \quad (\text{for } d = 2\text{m})$$

$$(b) \quad \underline{F} = - 3.14 (10^{-11}) \underline{i} \text{ N} \quad (\text{for } d = 4\text{m})$$

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$$mg = \frac{1}{2} mg_{h=0}$$

$$\frac{R^2}{(R+h)^2} g_0 = \frac{1}{2} g_0$$

Solve for  $h$  to obtain  $h = (\sqrt{2} - 1)R$

or  $h = 0.414R$

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$$\frac{1}{g} \quad g_h = \frac{Gm_e}{(R+h)^2}$$
$$= \frac{(3.439 \times 10^{-8})(4.095 \times 10^{23})}{[(3959)(5280) + (150)(5280)]^2} = \underline{29.9 \text{ ft/sec}^2}$$

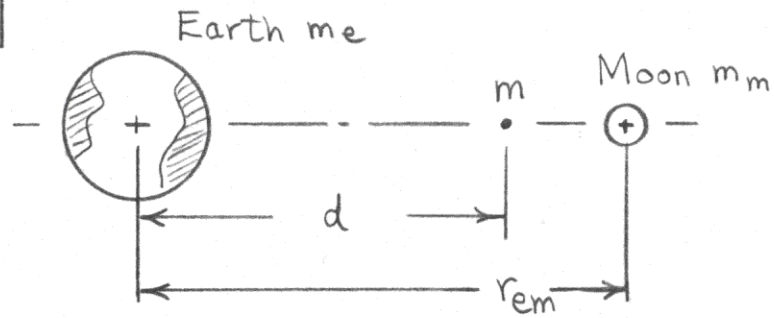
$$\text{Mass of man: } m = \frac{W}{g} = \frac{200}{32.174} = 6.22 \text{ slugs}$$

Absolute weight at  $h = 150$  miles:

$$W_h = mg_h = (6.22)(29.9) = \underline{186.0 \text{ lb}}$$

The terms "zero-g" and "weightless" are definitely misnomers in this instance.

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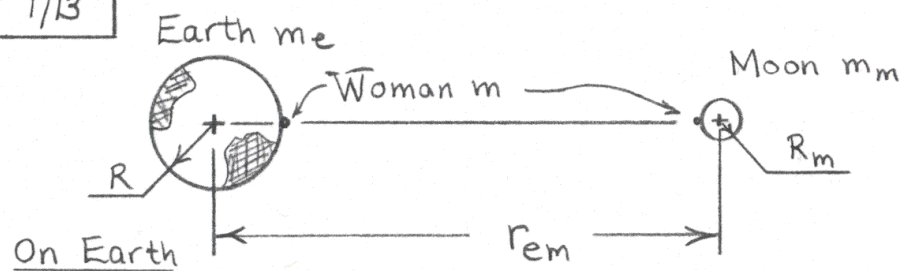
Newton's Law of Universal Gravitation:

$$\frac{G m_e m}{d^2} = \frac{G m_m m}{(r_{em} - d)^2} \Rightarrow m_m d^2 = m_e (r_{em} - d)^2$$

With  $m_m = 0.0123 m_e$  and  $r_{em} = 384\,398$  km,

$$\begin{cases} d = 346\,022 \text{ km} & (\text{between earth \& moon}) \\ d = 432\,348 \text{ km} & (\text{to right of moon}) \end{cases}$$

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$$F_e = \frac{Gm_em}{R^2} \quad F_m = \frac{Gm_mm}{(r_{em}-R)^2}$$

$$\text{Ratio } R_{em} = \frac{F_e}{F_m} = \frac{m_e (r_{em}-R)^2}{m_m R^2}$$

$$\begin{aligned} \text{or } R_{em} &= \frac{1}{0.0123} \frac{[384398 - 6371]^2}{[6371]^2} \\ &= \underline{\underline{286000}} \end{aligned}$$

On moon

$$F_e = \frac{Gm_em}{(r_{em}-R_m)^2} \quad F_m = \frac{Gm_mm}{R_m^2}$$

$$R_{em} = \frac{F_e}{F_m} = \frac{m_e R_m^2}{m_m (r_{em}-R)^2}$$

$$= \frac{1}{0.0123} \frac{[3476/2]^2}{[384398 - 3476/2]^2} = \underline{\underline{0.001677}}$$

(Note:  $R_{me} = F_m/F_e = 1/R_{em} = 596$ )

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$$mv = \int_{t_1}^{t_2} (F \cos \theta) dt$$
$$[M][LT^{-1}] = [MLT^{-2}][T]$$
$$[MLT^{-1}] = [MLT^{-1}] \quad \checkmark$$