Chapter 2 Questions

Multiple Choice Questions

1. In a recursive solution, the _____ terminates the recursive processing.
    a) local environment
    b) pivot item
    c) base case
    d) recurrence relation

    Answer: c.

2. A binary search uses a _____ strategy.
    a) divide-and-conquer
    b) sequential
    c) determine-the-pivot
    d) smallest-to-largest

    Answer: a.

3. A _____ is a mathematical formula that generates the terms in a sequence from previous terms.
    a) local environment
    b) pivot item
    c) base case
    d) recurrence relation

    Answer: d.

4. The factorial of n is equal to _____.
    a) $n - 1$
    b) $n -$ factorial $(n–1)$
    c) factorial $(n–1)$
    d) $n *$ factorial $(n–1)$

    Answer: d.

5. The base case for a recursive definition of the factorial of n is _____.
    a) factorial $(–1)$
    b) factorial (0)
    c) factorial (n)
    d) factorial $(n – 1)$

    Answer: b.

6. What is fundamentally wrong with computing the Fibonacci sequence recursively?
    a) it has two base cases
    b) each call to the function results in two recursive calls
    c) it computes the same values over and over
    d) nothing

    Answer: c.

7. In the box trace, each box roughly corresponds to a(n) _____.
    a) recursive relation
    b) activation record
    c) base case
    d) pivot item

    Answer: b.

8. In the box trace, each box contains all of the following EXCEPT _____.
    a) the values the function's arguments
    b) the function's local variables
    c) the function's execution time

d) a placeholder for the value returned by each recursive call from the current box
e) the value returned by the function itself

Answer: c.

9. In the box trace for a recursive function, a new box is created each time _____.
   a) the function is called
   b) the function returns a value
   c) an object is created
   d) an object is initialized

Answer: a.

10. What happens if a recursive function never reaches a base case?
   a) the function returns the correct value
   b) the function returns an incorrect value
   c) the function terminates immediately
   d) an infinite sequence of recursive calls occurs

Answer: d.

11. In a recursive method that writes a string of characters in reverse order, the base case is _____.
   a) a string with a length of 0
   b) a string whose length is a negative number
   c) a string with a length of 3
   d) a string that is a palindrome

Answer: a.

12. Which of the following is a precondition for a method that accepts a number n and computes the nth Fibonacci number?
   a) n is a negative integer
   b) n is a positive integer
   c) n is greater than 1
   d) n is an even integer

Answer: b.

13. How many bases cases does a recursive binary search of a sorted array have?
   a) 0
   b) 1
   c) 2
   d) 3

Answer: c.

14. The number of ways to choose k out of n things is _____.
   a) the number of ways to choose $k – 1$ out of $n – 1$ things
   b) the number of ways to choose k out of $n – 1$ things
   c) the sum of the number of ways to choose $k – 1$ out of $n – 1$ things and the number of ways to choose k out of $n – 1$ things
   d) the product of the number of ways to choose $k – 1$ out of $n – 1$ things and the number of ways to choose k out of $n – 1$ things

Answer: c.

15. When you solve a problem by solving two or more smaller problems, each of the smaller problems must be _____ the base case than the original problem.
   a) closer to
   b) farther to
   c) either closer to or the same "distance" from
   d) either farther to or the same "distance" from

Answer: a.

Chapter 2 Questions

16. A recursive method that computes the number of groups of *k* out of *n* things has the precondition that _____.
    a) *n* is a positive number and *k* is a nonnegative number
    b) *n* is a nonnegative number and *k* is a positive number
    c) *n* and *k* are nonnegative numbers
    d) *n* and *k* are positive numbers

Answer: c.

17. The midpoint of a sorted array has the index _____, where `first` is the index of the first item in the array, and `last` is the index of the last item in the array.
    a) `first / 2 + last / 2`
    b) `first / 2 - last / 2`
    c) `(first + last) / 2`
    d) `(first - last) / 2`

Answer: c.

18. If the value sought by a recursive binary search algorithm is in the array, which of the following is true?
    a) the algorithm makes the same comparisons as a sequential search
    b) the algorithm is successful without reaching a base case
    c) the algorithm searches the entire array
    d) the algorithm searches only the array half containing the value

Answer: d.

19. Which of the following is NOT a precondition for an array that is to be searched by a recursive binary search algorithm? (`first` is the index of the first item in the array, `last` is the index of the last item in the array, and `SIZE` is size of the array)
    a) `SIZE <= first`
    b) `0 <= first`
    c) `last <= SIZE - 1`
    d) `anArray[first] <= anArray[first + 1] <= … <= anArray[last]`

Answer: a.

20. What does the following recursive algorithm display?
```
writeBack(in s:string)
  if (s is empty)
    return
  else
  {
    Write the first character of s
    writeBack(the string beginning at the second character of s)
  }
```
    a) nothing
    b) the first character of s a number of times equal to the length of s
    c) the string s
    d) the string s backward

Answer: c.

21. For an array containing 2, 3, 5, 6, 9, 13, 16, and 19, what value does a recursive binary search algorithm return when it searches for 6?
    a) 1
    b) 3
    c) 4
    d) none of the above

Answer: b.

Chapter 2 Questions

22. For an array containing 2, 3, 5, 6, 9, 13, 16, and 19, what value does a recursive binary search algorithm return when it searches for 10?
    a) −1
    b) 0
    c) 1
    d) 10
Answer: a.

23. In a sorted array having `SIZE` locations, the kth smallest item is given by _____.
    a) `anArray[k-1]`
    b) `anArray[k]`
    c) `anArray[SIZE-k]`
    d) `anArray[SIZE+k]`
Answer: a.

24. A recursive binary search algorithm always reduces the problem size by _____ at each recursive call.
    a) 1
    b) 2
    c) half
    d) one-third
Answer: c.

25. A recursive solution that finds the factorial of *n* always reduces the problem size by _____ at each recursive call.
    a) 1
    b) 2
    c) half
    d) one-third
Answer: a.

26. In the recursive solution to finding the kth smallest item in an array, the problem size decreases by _____ at each recursive call.
    a) 1
    b) at least 1
    c) half
    d) at least half
Answer: b.

27. In the recursive solution to the Towers of Hanoi problem, the number of disks to move _____ at each recursive call.
    a) decreases by 1
    b) increases by 1
    c) decreases by half
    d) increases by half
Answer: a.

28. A recursive solution that finds the factorial of *n* generates _____ recursive calls.
    a) *n* - 1
    b) *n*
    c) *n* + 1
    d) *n* * 2
Answer: b.

29. In the Fibonacci sequence, which of the following integers comes after the sequence 1, 1, 2, 3?
    a) 3
    b) 4

        c) 5
        d) 6

Answer: c.

30. Which of the following is a base case for a recursive binary search algorithm?
    (`first` is the index of the first item in the array, `last` is the index of the last item in the array, and `mid` is the midpoint of the array).
    a) `last > first`
    b) `first > last`
    c) `0 <= first`
    d) `last <= SIZE-1`

Answer: b.

Chapter 2 Questions

True/False Questions

1. A recursive solution solves a problem by solving a smaller instance of the same problem.
Answer: True.

2. An iterative solution involves loops.
Answer: True.

3. A binary search starts at the beginning of the collection of items.
Answer: False.

4. An iterative method always calls itself.
Answer: False.

5. In practice, recursion should be used even when a problem has a simple iterative solution.
Answer: False.

6. When constructing a recursive solution, you should assume that a recursive call's postcondition is true if its precondition is true.
Answer: True.

7. Every recursive method must have a base case.
Answer: True.

8. A recursive solution can have more than one base case.
Answer: True.

9. The binary search algorithm can be applied to an unsorted array.
Answer: False.

10. The base case for a recursive solution to finding the kth smallest item in an array cannot be predicted in advance.
Answer: True.

Chapter 2 Questions

Short Answer Questions

1. What items does a sequential search examine when it is successful?
Answer: A sequential search starts at the beginning of the collection and looks at every item in the collection in order until the desired item is found.

2. What is a base case?
Answer: A base case is a special case of a recursive function whose solution you know. A base case enables the recursive processing to terminate.

3. What are the four questions that must be considered when constructing a recursive solution?
Answer: The four questions that must be considered when constructing a recursive solution are:
- How can you define the problem in terms of a smaller problem of the same type?
- How does each recursive call diminish the size of the problem?
- What instance of the problem can serve as the base case?
- As the problem size diminishes, will you reach this base case?

4. What is a recurrence relation?
Answer: A recurrence relation is a mathematical formula that generates the terms in a sequence from previous terms.

5. What is the box trace?
Answer: The box trace is a systematic way to trace the actions of a recursive method.

6. What is an activation record?
Answer: An activation record is a record that contains a method's local environment at the time of and as a result of the call to the method.

7. What elements are included in a method's local environment?
Answer: The local environment of a method includes the method's local variables, a copy of the actual value arguments, a return address in the calling routine, and the value of the method itself.

8. What are the two base cases for a recursive binary search algorithm?
Answer: The two base cases are:
- `first > last`
- `value == anArray[mid]`
where `first` is the index of the first item in the array `anArray`, `last` is the index of the last item in `anArray`, and `mid` is the midpoint of `anArray`.

9. When is the base case `first > last` (where `first` is the index of the first item in the array and `last` is the index of the last item in the array) reached in a recursive binary search algorithm?
Answer: This base case is reached when the value sought is not in the original array.

10. When is the base case `value == anArray[mid]` (where `mid` is the midpoint of the array) reached in a recursive binary search algorithm?
Answer: This base case is reached when the value sought is in the original array.

11. What is a pivot item?
Answer: A pivot item is an element of a data collection that an algorithm uses to arrange the rest of the collection.

12. What is the base case for the recursive solution to the Towers of Hanoi problem?
Answer: The base case for the recursive solution to the Towers of Hanoi problem is a tower containing only one disk.

13. What are the two factors that contribute to the inefficiency of some recursive solutions?

Chapter 2 Questions

Answer: The two factors are the overhead associated with method calls, and the inherent inefficiency of some recursive algorithms.

14. What is a tail-recursive function?

Answer: A tail-recursive function is a function whose last action is a recursive call.

15. Why do some compilers automatically replace tail recursion with iteration?

Answer: Some compilers automatically replace tail recursion with iteration because tail-recursive methods are often less efficient than their iterative counterparts, and the conversion of a tail-recursive method to an equivalent iterative method is rather mechanical.